USER'S MANUAL FOR THE RealGasBrine v1.0 Option of TOUGH+ v1.5: A Code for the Simulation of System Behavior in Gas-Bearing Geologic Media

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August 2014

This work was supported by the Assistant Secretary for Fossil Energy, Office of Natural Gas and Petroleum Technology, through the National Energy Technology Laboratory, under the U.S. Department of Energy, Contracts No. DE-AC03-76SF00098 and DE-AC02-05CH11231.

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Abstract

REALGASBRINE v1.0 is a numerical code that for the simulation of the behavior of gas-bearing porous and/fractured geologic media. It is an option of TOUGH+ v1.5 [*Moridis*, 2014], a successor to the TOUGH2 [*Pruess et al.*, 1999] family of codes for multi-component, multiphase fluid and heat flow developed at the Lawrence Berkeley National Laboratory. REALGASBRINE v1.0 needs the TOUGH+ v1.5 core code in order to compile and execute. It is written in standard FORTRAN 95/2003, and can be run on any computational platform (workstation, PC, Macintosh) for which such compilers are available.

REALGASBRINE v1.0 describes the non-isothermal two- (for pure water) or threephase (for brine) flow of an aqueous phase and a real gas mixture in a gas-bearing medium, with a particular focus in ultra-tight (such as tight-sand and shale gas) systems. Up to 12 individual real gases can be tracked, and salt can precipitate as solid halite. The capabilities of the code include coupled flow and thermal effects, real gas behavior, Darcy and non-Darcy flow, several isotherm options of gas sorption onto the grains of the porous media, complex fracture descriptions, gas solubility into water, and geomechanical effects on flow properties. REALGASBRINE v1.0 allows the study of flow and transport of fluids and heat over a wide range of time frames and spatial scales not only in gas reservoirs, but also in any problem involving the flow of gases in geologic media, including the geologic storage of greenhouse gas mixtures, the behavior of geothermal reservoirs with multi-component condensable (H₂O and CO₂) and noncondensable gas mixtures, the transport of water and released H₂ in nuclear waste storage applications, etc. PAGE LEFT INTENTIONALLY BLANK

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1.0. Introduction

1.1. Background

To a large part, the impetus for the development of the REALGASBRINE v1.0 application option was provided by the importance of ultra-tight natural gas reservoirs (such as shale gas reservoirs), production from which has virtually exploded over the last decade because of the advent of effective reservoir stimulation technologies. While the code has wide application to any problem involving the storage and flow of gases in geologic media, the linkage to tight gas reservoirs is obvious, as attested to by as some of the code features and capabilities (e.g., gas sorption and non-Darcy flows) that were introduced to address the particular needs of such reservoirs. Thus, the introduction cannot but address this subject.

The ever-increasing energy demand, coupled with the advent and advances in reservoir stimulation technologies, has prompted an explosive growth in the development of unconventional gas resources in the U.S. during the last decade. Tight-sand and shale gas reservoirs are currently the main unconventional resources, upon which the bulk of

production activity is currently concentrating (Warlick, 2006). Production from such resources in the U.S. has skyrocketed from virtually nil at the beginning of 2000, to 6% of the gas produced in 2005 (U.S. EIA, 2007), to 23% in 2010, and is expected to reach 49% by 2035 (U.S. EIA, 2012). Production of shale gas is expected to increase from a 2007 U.S. total of 1.4 TCF to 4.8 TCF in 2020 (API, 2013). In its Annual Energy Outlook for 2011, the US Energy Information Administration (EIA) more than doubled its estimate of technically recoverable shale gas reserves in the US from 353 TCF to 827 TCF by including data from recent drilling results in the Marcellus, Haynesville, and Eagle Ford shales (US EIA, 2011). Note that the bulk of the gas production from tight sands and shales has concentrated almost exclusively in North America (U.S. and Canada), and serious production elsewhere in the rest world has yet to begin. This leads to reasonable expectations that gas production from such ultra-tight systems may be one of the main sources (if not the main) source of natural gas in the world for decades to come, with obvious economic and geostrategic implications, and significant benefits for national economies and national energy security.

The importance of tight-sand and shale reservoirs as energy resources necessitates the ability to accurately estimate reserves and to evaluate, design, manage and predict production from such systems over a wide range of time frames and spatial scales. Modeling and simulation play a key role in providing the necessary tools for these activities. However, these reservoirs present challenges that cannot easily (if at all) handled by conventional gas models and simulators: they are characterized by extremely low permeabilities (often in the nD = 10^{-21} m² range), have native fractures that interact with the fractures created during the reservoir stimulation and with the matrix to result in very complicated flow regimes that very often deviate from Darcy's Law, have pores very small pores that interfere with the Brownian motion of the gas molecules (thus rendering predictions from standard advection-based models dubious, if not irrelevant, as they requiring accounting for Knudsen and multi-component diffusion), exhibit highly non-linear behavior, have large amounts of gas sorbed onto the grains of the porous media in addition to gas stored in the pores, and may exhibit unpredictable geomechanical behavior such as the evolution of secondary fractures (Kim and Moridis, 2013) that may further complicate an already complex flow regime.

Several analytical and semi-analytical models have been proposed to predict flow performance and production from these ultra-tight reservoirs [*Gringarten*, 1971; *Gringarten et al.*, 1974, *Blasingame and Poe*, 1993; *Medeiros et al.*, 2006; *Bello and Wattenbarger*, 2008; *Mattar*, 2008; *Anderson et al.*, 2010]. Most of these studies have assumed idealized and regular fracture geometries, include significant simplifying assumptions and cannot accurately handle the very highly nonlinear aspects of shale-gas and tight-gas reservoirs, cannot describe complex domain geometries, and cannot accurately capture gas sorption and desorption from the matrix (a non-linear process that does not lend itself to analytical solutions), multiphase flow, consolidation, and several non-ideal and complex fracture networks [*Houze et al.*, 2010]. Thus, their role as decision-making tools is limited, making numerical simulators the only practical option.

The economic importance of the energy resources in such ultra-tight reservoirs and the shortcomings of the analytical and semi-analytical models have led to the development of numerical reservoir simulators that address the particularities of these systems. *Miller et al.* [2010] and *Jayakumar et al.* [2011] used numerical simulation to history-match and

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forecast production from two different shale-gas fields. *Cipolla et al.* [2009], *Freeman* [2010], *Moridis et al.* [2010] and *Freeman et al.* [2009; 2013] and conducted numerical sensitivity studies to identify the most important mechanisms and factors that affect shale-gas reservoir performance.

Powerful commercial simulators with specialized options for shale gas analysis such as GEM [*CMG*, 2013] and ECLIPSE For Unconventionals [*SLB*, 2013] have become available. While these address the most common features of unconventional and ultra-tight media, they are designed primarily for large-scale production evaluation at the reservoir level and cannot be easily used for scientific investigations of micro-scale processes and phenomena in the vicinity of fractures.

The TOUGH+ v1.5 code with the REALGASBRINE v1.0 application (hereafter collectively referred to as **T+RGB**) described in this report is capable of simulating processes and phenomena of flow through a wide variety of geological media (from very permeable to ultra-tight, porous and fractured) over a range of scales that varies from the mm- to the field-level. This report describes underlying physics and thermodynamics of **T+RGB**, lists and explains the data inputs required for its application, and discusses several applications to problems of flow and transport in gas-bearing media.

1.2. The TOUGH+ Family of Codes

TOUGH+ v1.5 is a family of public domain codes developed at the Lawrence Berkeley National Laboratory [*Moridis*, 2015] as a successor to the TOUGH2 [*Pruess et al.*, 1991] family of codes for multi-component, multiphase fluid and heat flow. It employs dynamic

memory allocation, follows the tenets of Object-Oriented Programming (OOP), and involves entirely new data structures and derived data types that describe the objects upon which the code is based. It is written in standard FORTRAN 95/2003, and can be run on any computational platform (workstations, PC, Macintosh).

By using the capabilities of the FORTRAN95/2003 language, the new OOP architecture involves the use of pointers, lists and trees, data encapsulation, defined operators and assignments, operator extension and overloading, use of generic procedures, and maximum use of the powerful intrinsic vector and matrix processing operations (available in the extended mathematical library of FORTRAN 95/2003). This leads to increased computational efficiency, while allowing seamless applicability of the code to multi-processor parallel computing platforms. The result is a code that is transparent and compact, and frees the developer from the tedium of tracking the disparate attributes that define the objects, thus enabling a quantum jump in the complexity of problem that can be tackled. An additional feature of the FORTRAN 95/2003 language of TOUGH+ is the near complete interoperability with C/C++, which allows the interchangeable use of procedures written in either FORTRAN 95/2003 or C/C++, makes possible the seamless coupling with external packages (such as the geomechanical commercial code FLAC3D [*Itasca*, 2002]) and interaction with pre- and post-processing graphical environments.

TOUGH+ v1.5 has a completely modular architecture. Any member of the TOUGH+ family of codes comprises three components: (a) the core TOUGH+ code that is common to all applications related to the study of non-isothermal processes of flow and transport through geologic media, (b) the code that is *unique* to a particular type of application/problem (e.g., the properties and flow of a crude oil, the flow of water and air

through geologic media, etc.), and (c) supplemental TOUGH+ code units that describe special physics and processes that are encountered in particular types of problems (e.g., code units that describe real gas properties, non-Darcian flow processes, salinity effects on the properties of water, etc.) and are *used by more than one* application options.

Thus, the core TOUGH+ code – which is distributed as a separate entity by LBNL– cannot conduct any simulations by itself, but needs additional units of supplemental and problem-specific code before it can become operational. The additional code solves the equation of state (EOS) corresponding to the specific problem; it is called an *application option* or simply an *option* in the TOUGH+ nomenclature and is distributed as a separate entity/product by LBNL. The term *option* – rather the older term *module* or *EOS* that were used in the TOUGH2 [*Pruess et al.*, 1999] nomenclature – is used to avoid confusion, as the word *module* has a particular meaning in the FORTRAN 95/2003 language of TOUGH+.

1.3. The REALGASBRINE v1.0 Code

REALGASBRINE v1.0 is the TOUGH+ v1.5 application option that describes the nonisothermal two- (for pure water) or three-phase (for brine) flow of an aqueous phase and a real gas mixture in any type of gas bearing medium, with a particular focus in ultra-tight (such as tight-sand and shale gas) systems. The gas mixture is treated as either a singlepseudo-component having a fixed composition, or as a multicomponent system composed of up to 12 individual real gases, including CO_2 . In the case of brine, the salt can precipitate as solid halite under appropriate conditions, leading to reductions in porosity and permeability.

In addition to the standard capabilities of all members of the TOUGH+ family of codes (fully-implicit, compositional simulators using both structured and unstructured grids), the capabilities of the code include: coupled flow and thermal effects in porous and/or fractured media, real gas behavior, gas slippage (Klinkenberg) effects, full micro-flow treatment (Knudsen diffusion [*Freeman et al.*, 2011] and Dusty Gas Model [*Webb*, 1998]), Darcy and non-Darcy flow through the matrix and fractures of fractured media, single- and multi-component gas sorption onto the grains of the porous media following several isotherm options, discrete and equivalent fracture representation, porosity-permeability dependence on pressure changes, complex matrix-fracture relationships with generalized fracture effect concepts such as dual- and multi-porosity [*Warren and Root*, 1963], dual-permeability, and multiple interactive continua [*Pruess*, 1983; *Doughty et al.*, 1999], etc.. The code involves robust physics of gas dissolution into water/brine, and the most updated thermodynamics describing the behavior of gaseous components and water.

The **T+RGB** v1.0 code account for practically all known processes and phenomena, involve a minimum of assumptions, and are suitable for scientific investigations at any spatial (from the sub-mm scale in the vicinity of the fracture surface to the reservoir scale) and temporal scales, thus allowing insights into the system performance and behavior during production. It can provide solutions to the problem of prediction of gas production from the entire spectrum of gas-bearing reservoirs, but also of any reservoir involving water and gas mixtures of up to 12 components (including H₂O vapor). The code can simulate problems of any scale, ranging from mm-scale processes at the imbibing surface of a hydraulic fracture to core-scale studies to field-scale investigations. The only limitations on the size of the domain to be simulated are imposed by the underlying physics and by the capabilities of the computational platform. Thus, if the volume of the domain and its subdivision are such that (a) a representative volume can be defined and (b) the flow of fluids can be adequately described by a macro-scale model, then **T+RGB** can predict the system behavior.

Note that, although the main impetus for the development of \mathbf{T} +**RGB** was the need to analyze and understand the problems of flow of water/brine and hydrocarbon gases through tight reservoirs, it is important to indicate that the code is fully applicable to a wide variety of other problems, including the study of the geologic storage of greenhouse gas mixtures, the behavior of geothermal reservoirs with multi-component condensable (H₂O and CO₂) and non-condensable gas mixtures, the transport of water and released H₂ in nuclear waste storage applications, etc..

This report provides a detailed presentation of the features and capabilities of T+RGB, and includes a thorough discussion of the underlying physical, thermodynamic and mathematical principles of the model in addition to the main governing equations. The various phase regimes and the corresponding primary variables are discussed in detail, as well as the reasons for their selection. Examples of input data files, of the corresponding output files, as well as the results from these illustrative sample problems of gas production from realistic gas-bearing geologic systems, are included as an aide to the T+RGB user.

2.0 Concepts, Underlying Physics, and Governing Equations

2.1. Modeled Processes and Underlying Assumptions

T+RGB can model the following processes and phenomena in gas-bearing geologic systems:

- The flow of gases and liquids in the porous/fractured geologic system by Darcian and/or non-Darcian physics
- (2) The corresponding heat flow and transport
- (3) The partitioning of the mass components among the possible phases
- (4) Heat exchanges due to
 - a. Conduction
 - b. Advection/convection
 - c. Radiation
 - e. Latent heat related to phase changes (ice melting or water fusion, water evaporation or vapor condensation)

- f. Gas dissolution
- g. Salt dissolution
- (5) Gas sorption onto the grains of the porous media
- (6) The transport of salt in the aqueous phase, accounting for advection and molecular diffusion
- (7) The precipitation salt as halite if its concentration in the aqueous phase exceeds its solubility
- (8) The effects of salt on the thermophysical properties of water (density, viscosity, vapor pressure, enthalpy, etc.)

A deliberate effort was made to keep the simplifying assumptions involved in the development of the underlying physical, thermodynamic and mathematical model to a minimum. These include:

- Flow in the domain can be described by one or more of the Darcian and non-Darcian models available in T+RGB.
- (2) In the transport of dissolved gases and salts, mechanical dispersion is small compared to advection (by neglecting mechanical dispersion, memory requirements and execution times are substantially reduced).
- (3) The pressure P < 100 MPa (14,504 psi). The pressure-dependent equations describing the water properties and behavior in **T+RGB** provide accurate solutions for practically the entire spectrum of conditions encountered in natural geologic media. Thus, the existing capabilities can easily accommodate any natural or laboratory system. Although equations for an accurate description of the thermophysical properties of gas+H2O systems for *P* as high as 1000 MPa are

available in the code, this option is disabled because it involves an iterative process that increases the execution time by a factor of 3 or 4 even for P < 100 MPa.

2.2. Components and Phases

A non-isothermal gas + H₂O system can be fully described by the appropriate mass balance equations and an energy balance equation. The following components κ (and the corresponding indicators used in the subsequent equations), corresponding to the number of equations, are considered in **T**+**RGB**:

- $\kappa \equiv g^i$ the various gaseous components i ($i = 1, ..., N_G, N_G \ge 1$) constituting the gas mixture.
 - w water
 - s salt
 - θ heat

The following 12 gases are available in T+RGB: CH₄, C₂H₆, C₃H₈, n-C₄H₁₀, i-C₄H₁₀, H₂O, CO₂, H₂S, O₂, N₂ C₂H₅OH, and H₂, of which only H₂O, CO₂ and C₂H₅OH are condensable. These are included as standard entries into the database of the TOUGH+ v1.5 supplemental code unit **T_RealGas_Properties.f95** [*Moridis*, 2014].

In **T+RGB**, if the circumstances warrant it, it is possible to treat the H₂O-free part of a real gas mixture as a *single pseudo-component* (i.e., $N_G = 1$) of constant composition (i.e., with non-variant mole fractions Y^i of the individual gases), the properties of which vary with the pressure P and temperature T. In that case, the gas phase comprises two components: the H₂O and the H₂O-free pseudo-component. The composition of the gas phase may still change (because of the near-universal presence of H_2O vapor in the subsurface), but the composition of the individual gases that constitute the pseudo-component is treated as invariant. Air is a good example of such a pseudo-component for **T+RGB** applications.

Note that heat is included in this list as a pseudo-component (as the heat balance is tracked similarly to the mass balance of the individual mass components) for the purpose of defining the maximum number of simultaneous equations to be solved. Thus, the list indicates that the maximum number of mass components that may be considered in a problem involving pure water and a gas mixture of N_G constituents is N_G +1; for a brine, the number of mass components is N_G +2. The corresponding maximum number of simultaneous equations that need to be solved is $N_E = N_G$ (for isothermal conditions) and $N_E = N_G$ +1.

These mass and energy components are partitioned among four possible phases β , which are listed below along with the corresponding indicators (used in the subsequent equations):

- $\beta \equiv H$ solid: precipitated halite (components: s)
 - A aqueous (components: liquid w, dissolved s, N_G dissolved gases)
 - G gaseous (components: N_G gases, vapor w)

2.3. The Mass and Energy Balance Equation

Following *Pruess et al.* [1999], mass and heat balance considerations in every subdomain (gridblock) into which the simulation domain is been subdivided by the integral finite difference method dictates that

$$\frac{d}{dt} \int_{V_n} M^{\kappa} dV = \int_{\Gamma_n} \mathbf{F}^{\kappa} \cdot \mathbf{n} \, d\tilde{A} + \int_{V_n} q^{\kappa} dV, \qquad (2.3)$$

where:

V, V_n volume, volume of subdomain $n[L^3]$;

- M^{κ} mass accumulation term of component κ [kg m⁻³];
- A, Γ_n surface area, surface area of subdomain $n[L^2]$;
- \mathbf{F}^{κ} Darcy flux vector of component κ [kg m⁻²s⁻¹];
- **n** inward unit normal vector;
- q^{κ} source/sink term of component κ [kg m⁻³s⁻¹];

t time [T].

2.4. Mass Accumulation Terms

Under equilibrium conditions, the mass accumulation terms M^{κ} for the mass components in equation (2.3) are given by

$$M^{\kappa} = \sum_{\beta \equiv A, G, H} \phi S_{\beta} \rho_{\beta} X^{\kappa}_{\beta} + \delta^{i}_{\Psi} (1 - \phi) \rho_{R} \Psi^{i}, \quad \kappa \equiv w, g^{i}, s, \quad i = 1, \dots, N_{G}$$
(2.4)

where

 ϕ porosity [*dimensionless*];

 ρ_{β} density of phase β [kg m⁻³];

- S_{β} saturation of phase β [dimensionless];
- X_{β}^{κ} mass fraction of component $\kappa \equiv w, m, i$ in phase β [kg/kg]
- Ψ^i the mass of sorbed component g^i per unit mass of rock [kg/kg]
- $\delta_{\Psi}^{i} = 0$ for non-sorbing species on a given medium (including tight-gas systems) that are usually devoid of substantial organic carbon; $\delta_{\Psi}^{i} = 1$ in gas-sorbing species onto a given medium. Obviously, $\delta_{\Psi}^{s} = 0$.

The first term in Equation (2.4) describes fluid mass stored in the pores, and the second the mass of gaseous components sorbed onto the organic carbon (mainly kerogen) content of the matrix of the porous medium. The latter is quite common in shales. Although gas desorption from kerogen has been studied extensively in coalbed CH₄ reservoirs, and several analytic/semi-analytic models have been developed for such reservoirs [*Clarkson and Bustin*, 1999], the sorptive properties of shale are not necessarily analogous to coal [*Schettler and Parmely*, 1991].

The most commonly used empirical model describing sorption onto organic carbon in shales is analogous to that used in coalbed methane and follows the Langmuir isotherm that, for a single-component gas, is described by

$$\begin{cases} \Psi^{i} = \frac{p_{dG}m_{L}}{p_{dG} + p_{L}} \text{ for ELaS} \\ \frac{d\Psi^{i}}{dt} = k_{L} \left(\frac{p_{dG}m_{L}}{p_{dG} + p_{L}} - \Psi^{i}\right) \text{ for KLaS} \end{cases}, \qquad (2.5)$$

where p_{dG} is the dry gas pressure ($p_{dG} = p_G - p^v$, where p^v is the partial pressure of the water vapor), ELaS indicates Equilibrium Langmuir Sorption, and KLaS denotes Kinetic Langmuir Sorption. The m_L term in Equation (2.5) describes the total mass storage of component g^i at infinite pressure (kg of gas/kg of matrix material), p_L is the pressure at which half of this mass is stored (Pa), and k_L is a kinetic constant of the Langmuir sorption (1/s). In most studies, an *instantaneous equilibrium* is assumed to exist between the sorbed and the free gas, i.e., there is no transient lag between pressure changes and the corresponding sorption/desorption responses and the equilibrium model of Langmuir sorption is assumed to be valid. Although this appears to be a good approximation in shales [*Gao et al.*, 1994] because of the very low permeability of the matrix (onto which the various gas components are sorbed), the subject has not been fully investigated.

For multi-component gas, equation (3) becomes

$$\begin{bmatrix}
\Psi^{i} = \frac{p_{dG}B^{i}m_{L}^{i}\Upsilon^{i}}{1 + p_{dG}\sum_{i}B^{i}\Upsilon^{i}} & \text{for ELaS} \\
\frac{d\Psi^{i}}{dt} = k_{L}^{i} \left(\frac{p_{dG}B^{i}m_{L}^{i}\Upsilon^{i}}{1 + p_{dG}\sum_{i}B^{i}\Upsilon^{i}} - \Psi^{i}\right) & \text{for KLaS}
\end{bmatrix}$$
(2.6)

where B^i is the Langmuir constant of component g^i in 1/Pa (Pan et al., 2008), and Y^i is the dimensionless mole fraction of the gas component *i* in the water-free gas phase. Note that the **T+RGB** code offers the additional options of linear and Freundlich sorption isotherms (equilibrium and kinetic). For each gas component g^i , these are described by the following equations:

$$\begin{bmatrix} \Psi^{i} = K_{l}^{i} p^{i} & \text{for ELiS} \\ \frac{d\Psi^{i}}{dt} = k_{l}^{i} \left(K_{l}^{i} p^{i} - \Psi^{i} \right) & \text{for KLiS} \end{bmatrix} \text{ and } \begin{bmatrix} \Psi^{i} = K_{F}^{i} \left(p^{i} \right)^{c} & \text{for EFS} \\ \frac{d\Psi^{i}}{dt} = k_{F}^{i} \left[K_{F}^{i} \left(p^{i} \right)^{c} - \Psi^{i} \right] & \text{for KFS} \end{bmatrix}$$
(2.7)

where ELiS and KLiS denote Equilibrium and Kinetic Linear Sorption, respectively; EFS and KFS denote Equilibrium and Kinetic Freundlich Sorption, respectively; K_l^i and K_F^i are the distribution coefficients of the ELiS and EFS sorption isotherms of gas component *i*, respectively; p^i is the partial pressure of g^i ; k_l^i and k_F^i are the kinetic coefficients of the ELiS and EFS sorption isotherms of g^i , respectively; and c is the exponent of the Freundlich sorption isotherm

2.5. Heat Accumulation Terms

The heat accumulation term includes contributions from the rock matrix and all the phases, and, in the kinetic model, is given by the equation

$$M^{\theta} = (1 - \phi)\rho_{R} \int_{Tref}^{T} C_{R}(T) dT + \sum_{\beta = A,G,H} \phi S_{\beta}\rho_{\beta}U_{\beta} + \delta_{\Psi}^{i}(1 - \phi)\rho_{R} \sum_{i=1}^{N_{G}} u^{i}\Psi^{i}, \quad (2.8)$$

where

 ρ_R rock density [kg m⁻³];

- C_R heat capacity of the dry rock [J kg⁻¹K⁻¹];
- $U\beta$ specific internal energy of phase β [J kg⁻¹];
- u^i specific internal energy of sorbed gas component g^i [J kg⁻¹];
- *T_{ref}* a reference temperature [k];

The specific internal energy of the gaseous phase is a very strong function of composition, is related to the specific enthalpy of the gas phase H_G , and is given by

$$U_{G} = \sum_{\kappa = w, g^{i}(i=1, N_{G})} X_{G}^{\kappa} u^{\kappa} + U_{dep} \left(= H_{G} - \frac{P}{\rho_{G}} \right),$$
(2.9)

where u_G^{κ} is the specific internal energy of component κ in the gaseous phase, and U_{dep} is the specific internal energy departure of the gas mixture [J kg⁻¹].

The internal energy of the aqueous phase accounts for the effects of gas and salt solution, and is estimated from

$$U_{A} = X_{A}^{w} u^{w} + \sum_{i=1}^{N_{G}} X_{A}^{g^{i}} \left(u^{i} + U_{sol}^{i} \right), \qquad (2.10)$$

where u_A^w and u_A^i are the specific internal energies of the H₂O and of the natural gas component g^i at the p and T conditions of the aqueous phase, respectively, and U_{sol}^i are the specific internal energies of dissolution of the gas component g^i in H₂O (obtained from tables). Note that the reference state for all internal energy and enthalpy computations are p = 101300 Pa and T = 273.15 K (0 °C).

The salt-related term u_A^s and U_H are determined from

$$u_{A}^{s} = h_{A}^{s} - \frac{P}{\rho_{i}} = \int_{T_{ref}}^{T} C_{s} dT - \frac{P}{\rho_{s}} \text{ and } U_{H} = H_{H} - \frac{P}{\rho_{H}} = \int_{T_{ref}}^{T} C_{H} dT - \frac{P}{\rho_{H}}$$
(2.11)

where T_0 is a reference temperature, h_A^s and H_H are the specific enthalpies of the salt and halite (phase), respectively, and C_i and C_H are the temperature-dependent heat capacities of the salt and the halite, respectively [J kg⁻¹ K⁻¹].

2.6. Flux Terms

The mass fluxes of water, gases and salt include contributions from the aqueous and gaseous phases, i.e.,

$$\mathbf{F}^{\kappa} = \sum_{\beta \equiv A,G} \mathbf{F}^{\kappa}_{\beta}, \ \kappa \equiv w, g^{i}, \ i = 1, ..., N_{G}$$
(2.12)

Because it is immobile, the contribution of the solid phase ($\beta \equiv H$) to the fluid fluxes is zero. For any mobile phase β , $\mathbf{F}_{\beta}^{\kappa} = X_{\beta}^{\kappa} \mathbf{F}_{\beta}$.

In **T+RGB** there are three options to describe the phase flux \mathbf{F}_{β} . The first is the standard Darcy's law, i.e.,

$$\mathbf{F}_{\beta} = \rho_{\beta} \left[-\frac{k \, k_{r\beta}}{\mu_{\beta}} \nabla \Phi_{\beta} \right] = \rho_{\beta} \mathbf{v}_{\beta}, \quad \nabla \Phi_{\beta} = \nabla p_{\beta} - \rho_{\beta} \mathbf{g}, \tag{2.13}$$

where

k rock intrinsic permeability $[m^2]$;

 k_{rA} relative permeability of the aqueous phase [dimensionless];

 μ_A viscosity of the aqueous phase [Pa s];

P^A pressure of the aqueous phase [Pa];

g gravitational acceleration vector $[m s^{-2}]$.

In **T+RGB**, the relationship between the aqueous and the gas pressures, p_A and p_G , respectively, is given

$$P_A = P_G + P_{cGW}$$
, where $P_G = \sum_{i=1,...,N_G} P_G^i + P_G^w$ (2.14)

is the gas pressure [Pa], P_{cGW} is the gas-water capillary pressure [Pa], and P_G^i , P_G^w are the partial pressures [Pa] of the gas g^i and of the water vapor in the gas phase, respectively.

In **T**+**RGB**, the gas solubility in the aqueous phase cannot be satisfied by the simple approach of using Henry's law with a T-dependent Henry's coefficient that is standard in TOUGH+ v1.5 [*Moridis*, 2014] because this would lead to erroneous results when multi-component gases dissolve into brines. Thus, the much more involved option of determining the solubility by determining the chemical activities of the solution and by invoking the equality of in the aqueous and the gas phase.

The mass flux of the gaseous phase ($\beta \equiv G$) incorporates advection and diffusion contributions, and is given by

$$\mathbf{F}_{G}^{\kappa} = -k_{0} \left(1 + \frac{b}{P_{G}} \right) \frac{k_{rG} \rho_{G}}{\mu_{G}} X_{G}^{\kappa} \left(\nabla P_{G} - \rho_{G} \mathbf{g} \right) + \mathbf{J}_{G}^{\kappa}, \quad \kappa \equiv w, g^{i}$$
(2.15)

where

 k_0 absolute permeability at large gas pressures (= k) [m²];

b Klinkenberg [1941] *b*-factor accounting for gas slippage effects [Pa];

*k*_{rG} relative permeability of the gaseous phase [*dimensionless*];

 μG viscosity of the gaseous phase [Pa s].

Methods to estimate the *b*-factor are discussed in Section 4.

The term \mathbf{J}_{G}^{κ} is the diffusive mass flux of component κ in the gas phase [kg/m²/s], and is described by

$$\mathbf{J}_{G}^{\kappa} = -\phi S_{G} \underbrace{\left(\phi^{\frac{1}{3}} S_{G}^{\frac{7}{3}} \right)}_{\tau_{G}} D_{G}^{\kappa} \rho_{G} \nabla X_{G}^{\kappa} = -\phi (\tau_{G}) D_{G}^{\kappa} \rho_{G} \nabla X_{G}^{\kappa}, \quad \kappa \equiv w, m$$
(2.16)

where D_G^{κ} is the multicomponent molecular diffusion coefficient of component κ in the gas phase in the absence of a porous medium $[m^2 \text{ s}^{-1}]$, and τ_G is the gas tortuosity [dimensionless]. Several methods to compute τ_G are discussed by *Moridis* [2014]. The diffusive mass fluxes of the water vapor and of the g^i ($i = 1, ..., N_G$) gases are related through the relationship of *Bird et al.* [1960]

$$\mathbf{J}_{G}^{w} + \sum_{i=1,\dots,N_{G}} \mathbf{J}_{G}^{i} = \mathbf{0}, \qquad (2.17)$$

which ensures that the total diffusive mass flux of the gas phase is zero with respect to the mass average velocity when summed over the N_G +1 components. Then the total gas phase mass flux is the product of the Darcy velocity and density of the gas phase.

The flux of the dissolved salt is described by

$$\mathbf{F}_{A}^{s} = X_{A}^{s} \mathbf{F}_{A} + \mathbf{J}_{W}^{s}, \qquad (2.18)$$

where

$$\mathbf{J}_{W}^{s} = -\phi S_{W}\left(\phi^{\frac{1}{3}}S_{A}^{\frac{7}{3}}\right) D_{A}^{s}\rho_{A}\nabla X_{A}^{s} = -\phi S_{W}\left(\tau_{A}\right) D_{A}^{s}\rho_{A}\nabla X_{A}^{s}, \qquad (2.19)$$

 D_A^i is the molecular diffusion coefficient of salt in water, and τ_A is the medium tortuosity of the aqueous phase.

If the flow is non-Darcian because of inertial (turbulent) effects, then the equation $\mathbf{F}_{\beta} = \rho_{\beta} \mathbf{v}_{\beta}$ still applies, but \mathbf{v}_{β} is now computed from the solution of the quadratic equation

$$\nabla \Phi_{\beta} = -\left(\frac{\mu_{\beta}}{k k_{r\beta}} \mathbf{v}_{\beta} + \beta_{F\beta} \rho_{\beta} \mathbf{v}_{\beta} \Big| \mathbf{v}_{\beta} \Big|\right), \qquad (2.20)$$

in which β_{β} is the "turbulence correction factor" (Katz et al., 1959). The quadratic equation in (2.20) is the general momentum-balance *Forcheimer equation* [*Forchheimer*, 1901; *Wattenbarger and Ramey*, 1968], and incorporates inertial and turbulent effects. This is the second option. The solution then is

$$\mathbf{v}_{\beta} = \frac{2\nabla\Phi_{\beta}}{\frac{\mu_{\beta}}{k_{r\beta}} + \sqrt{\left(\frac{\mu_{\beta}}{k_{r\beta}}\right)^{2} + 4\beta_{F\beta}\rho\left|\nabla\Phi_{\beta}\right|}},$$
(2.21)

and the \mathbf{v}_{β} from equation (2.21) is then used in the equation of flow (2.13). **T+RGB** offers 13 options to compute $\beta_{F\beta}$ several of which are listed in *Finsterle* [2001]. The third option follows the approach of *Barree and Conway* [2007], as described by *Wu et al.* [2011], which involves a different formulation of $\nabla \Phi_{\beta}$.

The heat flux accounts for conduction, advection and radiative heat transfer, and is given by

$$\mathbf{F}^{\theta} = -\overline{k}_{\theta} \nabla T + f_{\sigma} \sigma_0 \nabla T^4 + \sum_{\beta = A, G} h_{\beta} \mathbf{F}_{\beta}, \qquad (2.22)$$

where

 \overline{k}_{θ} composite thermal conductivity of the medium/fluid ensemble [W m⁻¹ K⁻¹];

$$h_{\beta}$$
 specific enthalpy of phase $\beta \equiv A, G[J \text{ kg}^{-1}];$

 f_{σ} radiance emittance factor [dimensionless];

 σ_0 Stefan-Boltzmann constant [5.6687×10⁻⁸ J m⁻² K⁻⁴].

Several options to estimate \overline{k}_{θ} are discussed in *Moridis* [2014].

The specific enthalpy of the gas phase is computed as

$$H_G = \sum_{\kappa \equiv w, g^i} X_G^{\kappa} h_G^{\kappa} + H_{dep}, \qquad (2.23)$$

where h_G^{κ} is the specific enthalpy of component κ in the gaseous phase, and H_{dep} is the specific enthalpy departure of the gas mixture [J kg⁻¹]. The specific enthalpy of the aqueous phase is estimated from

$$H_{A} = X_{A}^{w} h_{A}^{w} + \sum_{\kappa=1,\dots,N_{d\kappa}} X_{A}^{\kappa} \left(h_{A}^{\kappa} + H_{sol}^{\kappa} \right), \qquad (2.24)$$

where $N_{d\kappa}$ is the total number of *dissolved* components (including the salt, if present), h_A^{κ} are the specific enthalpies of various dissolved components at the conditions prevailing in

the aqueous phase, respectively, and H_{sol}^{κ} is the specific enthalpy of dissolution [J kg⁻¹] of component κ in the aqueous phase, respectively.

2.7. Source and Sink Terms

In sinks with specified mass production rate, withdrawal of the mass component κ is described by

$$\hat{q}^{\kappa} = \sum_{\kappa=A,G} X^{\kappa}_{\beta} q_{\beta}, \quad \kappa \equiv w, g^{i}, s, \quad i = 1, ..., N_{G}$$

$$(2.25)$$

where q_{β} is the production rate of the phase β [kg m⁻³]. For a prescribed production rate, the phase flow rates q_{β} are determined internally according to the general different options available in the TOUGH+ code (see *Moridis* [2014]). For source terms (well injection), the addition of a mass component κ occurs at desired rates \hat{q}^{κ} ($\kappa \equiv w, g^{i}, s$). Salt injection can occur either as a rate as an individual mass component (\hat{q}^{i}) or as a fraction of the aqueous phase injection rate, i.e., $\hat{q}^{i} = X_{A}^{i} \hat{q}_{A}$, where X_{A}^{i} is the salt mass fraction in the injection stream.

The rate of heat removal or addition includes contributions of (a) the heat associated with fluid removal or addition, as well as (b) direct heat inputs or withdrawals q_d (e.g., microwave heating), and is described by

$$\hat{q}^{\theta} = q_d + \sum_{\beta=A,G} h_{\beta} q_{\beta}$$
(2.26)

2.8. Micro-Flows

2.8.1. Knudsen Diffusion and the Dusty Gas Model

For ultra-low permeability media (e.g., tight sands and shales) and the resulting microflows, **T+RGB** estimates a Klinkenberg *b*-factor for a single-component or pseudocomponent gas by the method of *Florence et al.* [2007] and *Freeman et al.* [2011] as

$$\frac{b}{P_G} = \left(1 + \alpha_K K_n\right) \left(1 + \frac{4K_n}{1 + K_n}\right) - 1,$$
(2.27)

where K_n is the Knudsen diffusion number (dimensionless), which characterizes the deviation from continuum flow, accounts for the effects of the mean free path of gas molecules $\overline{\lambda}$ being on the same order as the pore dimensions of the porous media, and is computed from [*Freeman et al.*, 2011] as

$$K_n = \frac{\overline{\lambda}}{r_{pore}} = \frac{\mu_G}{2.81708 p_G} \sqrt{\frac{\pi RT}{2M} \frac{\phi}{k}},$$
(2.28)

with *M* being the molecular weight and *T* the temperature (K). The term a_K in Eq. 24 is determined from Karniadakis and Beskok (2001) as

$$\alpha_{K} = \frac{128}{15\pi^{2}} \tan^{-1} \left(4K_{n}^{0.4} \right), \qquad (2.29)$$

For simplicity, we have omitted the "*i*" superscript in Equations (27) to (29). The Knudsen diffusion can be very important in porous media with very small pores (on the order of a few micrometers or smaller) and at low pressures. For a single gas pseudo-component, the properties in (29) are obtained from an appropriate equation of state for a real-gas mixture of constant composition Y^i . The Knudsen diffusivity D_K [m²/s] can be computed as proposed by *Civan* [2008] and *Freeman et al.* [2011].

$$D_{K} = \frac{4\sqrt{k\phi}}{2.81708} \sqrt{\frac{\pi RT}{2M}} \text{ or } D_{K} = \frac{kb}{\mu_{G}}$$
 (2.30)

2.8.1. Dusty Gas Model

For a multicomponent gas mixture that is not treated as a single pseudo-component, ordinary Fickian diffusion must be taken into account as well as Knudsen diffusion. Use of the advective–diffusive flow model (Fick's law) should be restricted to media with $k \ge 10^{-12}$ m²; the dusty-gas model (DGM) is more accurate at lower *k* [*Webb*, 1983; *Webb and Pruess*, 2003]. Additionally, DGM accounts for molecular interactions with the pore walls in the form of Knudsen diffusion. Shales may exhibit a permeability *k* as low as 10^{-21} m², so the DGM described below is more appropriate than the Fickian model [*Webb and Pruess*, 2003; *Doronin and Larkin*, 2004; *Freeman et al.*, 2011]:

$$\sum_{j=1,j\neq i}^{N_{G}} \frac{Y^{i} N_{D}^{j} - Y^{j} N_{D}^{i}}{D_{e}^{ij}} - \frac{N_{D}^{i}}{D_{K}^{i}} = \frac{p^{i} \nabla Y^{i}}{ZRT} + \left(1 + \frac{kp}{\mu_{G} D_{K}^{i}}\right) \frac{Y^{i} \nabla p^{i}}{ZRT}$$
(2.31)

where N_D^i is the molar flux of component g^i [mole m⁻²s⁻¹], D_e^{ij} is the effective gas (binary) diffusivity of species g^i in species g^j , and D_K^i is the Knudsen diffusivity of species g^i .

2.9. Salinity Effects on the Properties of the Aqueous Phase

The effects of salinity on the properties of the aqueous phase are fully described in the supplemental code unit **T_Saliity_Effects.f95** of TOUGH+ v1.5. Thus, the effect on the viscosity is described using correlations developed by *Phillips et al.* [1981] and by

Mao and Duan [2009]. The effect on density is computed from an estimate of the critical brine saturation [*Sourirayan and Kennedy*, 1992] and one of the following available methods: *Michaelides* [1981], *Miller* [1978] or *Lorenz* [2000]. The effect on the vapor pressure is quantified by the relationships and process proposed by *Haas* [1976]. The salt concentration at the point of precipitation is estimated using the method of *Chou* [1987]. Finally, the halite density and enthalpy are computed using the method of *Silvester and Pitzer* [1978].

The computational process to estimate these properties is quite involved, and falls beyond the scope of this report. The interested user is directed to the publications of these authors for a detailed description of their methods.

2.10. Other Processes, Properties, Conditions, and Related Numerical Issues

All other processes needed to complete the description of the fluid flows and system behavior in gas-bearing geologic media are common to most problems of flow and heat flow through porous/fractured media, are fully covered in the description of the core TOUGH+ code [*Moridis*, 2014], and will not be repeated here. These include issues related to relative permeability, capillary pressure, treatment of fractured media, as well as the space and time discretization, the Newton-Raphson method and the use of the Jacobian in the fully implicit solution of these problems (the standard approach in all TOUGH+ applications). The interested reader is directed to *Moridis* [2014] for a detailed discussion of all these subjects.

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3.0. Design and Implementation of the T+RGB Code

3.1. Primary Variables

The thermodynamic state and the distribution of the mass components among the two or three possible phases are determined from the gas + H₂O + salt equation of state. Following the standard approach employed in the TOUGH2 [*Pruess et al.*, 1999] family of codes, in **T+RGB** the system is defined uniquely by a set of N_{κ} primary variables (where κ denotes the number of mass and heat components under consideration, see Section 2.2) that completely specifies the thermodynamic state of the system.

Although the number N_{κ} of the primary variables is initially set at the maximum expected in the course of the simulation and does not change during the simulation, the thermodynamic quantities used as primary variables can change in the process of

simulation to allow for the seamless consideration of emerging or disappearing phases and components.

A total of 3 states (phase combinations) covering the entire possible phase if T > 0.01 °C and salt is not present are described in **T+RGB**; the number increases to 6 states when salinity is considered. The primary variables used for the various phase states without salt are listed in **Tables 3.1** and **3.2**, respectively. For systems with salinity, the additional primary variable is X_s_A , (corresponding to X_A^s , i.e., the mass fraction of salt in the aqueous phase). The primary variables in **Tables 3.1** and **3.2** are necessary and sufficient to uniquely define the H₂O-gas mixture-salt system.

3.2. Compiling the T+RGB Code

T+RGB is written in standard FORTRAN 95/2003. It has been designed for maximum portability, and runs on any computational platform (Unix and Linux workstations, PC, Macintosh) for which such compilers are available. Running **T+RGB** involves compilation and linking of the following code units and in the following order:

(4) T_RealGasBrine_Definitions.f95 (*)

Code unit providing default parameter values describing the basic attributes of the equation of state (i.e., number of components, number of phases, etc.)

(5) T_Allocate_Memory.f95

Code unit responsible for the dynamic memory allocation (following input describing the size of the problem) and dimensioning of most arrays needed by the code, in addition to memory deallocation of unnecessary arrays.

Phase	State Identifier	Primary Variable 1	Primary Variables 2,, N _G	Primary Variable N _G +1	Primary Variable N _G +2 (*)
1-Phase: G	Gas	P_gas	$Y_i_G, i=1,,N_G-1$	$Y_N_G_G$	Т
1-Phase: A	Aqu	Р	$X_i_A, i=1,, N_G-1$	$X_N_G_G$	Т
2-Phase: A+G	AqG	P_gas	$Y_i_G, i=1,,N_G-1$	S_aqu	Т

Table 3.1. Primary Variables in T+RGB Simulations without Salt.

The possible primary variables are: P, pressure [Pa]; P_gas , gas pressure [Pa]; T, temperature [C]; X_iA , mass fraction of gas i ($i=1,...,N_G$) dissolved in the aqueous phase [-]; Y_iA , mass fraction of gas i ($i=1,...,N_G$) dissolved in the aqueous phase [-]; S_aqu , liquid saturation [-]

 $N_E = N_G + 2$: maximum possible number of equations.

*For non-isothermal simulations only. For isothermal simulations, T is used to compute the thermophysical properties but is not part of the solution vector (i.e., the heat balance equation is not solved).

Phase	State Identifier	Primary Variable 1	Primary Variables 2, , N _G +1	Primary Variable N _G +2	Primary Variable N _G +3 (*)
1-Phase: G	Gas	P_gas	$Y_i_G, i=1,,N_G$	X_s_G	Т
1-Phase: A	Aqu	Р	$X_i_A, i=1,, N_G$	X_s_A	Т
2-Phase: A+G	AqG	P_gas	$\begin{array}{c} Y_i_G, i=1, \dots, N_G-1, \\ S_gas \end{array}$	X_s_A	Т
2-Phase: A+H	AqH	Р	$X_i_A, i=1,, N_G$	S_aqu	Т
2-Phase: H+G	GsH	P_gas	$Y_i_G, i=1,,N_G$	S_gas	Т
3-Phase: A+H+G	AGH	P_gas	$\begin{array}{c} Y_i_G, i=1, \dots, N_G-1, \\ S_aqu \end{array}$	S_gas	Т

 Table 3.2. Primary Variables in T+RGB Simulations With Salt.

The possible primary variables are: P, pressure [Pa]; P_gas , gas pressure [Pa]; T, temperature [C]; X_iA , mass fraction of gas i ($i=1,...,N_G$) dissolved in the aqueous phase [-]; Y_iG , mass fraction of gas i ($i=1,...,N_G$) dissolved in the gas phase [-]; S_aqu , liquid saturation [-]; S_gas , gas saturation [-]; X_sA , salt mass fraction in the aqueous phase [-].

 $N_E = N_G + 3$: maximum number of possible equations

*For non-isothermal simulations only. For isothermal simulations, T is used to compute the thermophysical properties but is not part of the solution vector (i.e., the heat balance equation is not solved).

(3) T Utility Functions.f95

Code unit that includes utility functions, i.e., a wide variety of mathematical functions, table interpolation routines, sorting algorithms, etc.).

(4) T_H2O_Properties.f95

Code unit that includes (a) all the water-related constants (parameters), and (b) procedures describing the water behavior and thermophysical properties/processes in its entire thermodynamic phase diagram.

(5) T_Media_Properties.f95

Code unit that describes the hydraulic and thermal behavior of the geologic medium (porous or fractured), i.e., capillary pressure and relative permeability under multiphase conditions, interface permeability and mobility, and interface thermal conductivity.

(6) T_RealGas_Properties.f95 (#)

Code unit that includes (a) the important constants (parameters) that are needed for the estimation of the properties of the various gases (see below), and (b) procedures describing the equation of state (EOS) of real gases (pure or mixtures) using any of the Peng-Robinson, Redlich-Kwong, or Soave-Redlich-Kwong cubic EOS model. The procedures in this code unit compute the following parameters and processes: compressibility, density, fugacity, enthalpy (ideal and departure), internal energy (ideal and departure), entropy (ideal and departure), thermal conductivity, viscosity, binary diffusion coefficients, solubility in water, and heat of dissolution in water.

(7) T_Salinity_Effects.f95 (#)

Code unit that computes all necessary properties and parameters in application options that involve salinity (e.g., brines). It estimates the salt solubility in H_2O , the halite density and enthalpy, the effect of salinity on

the density, viscosity and enthalpy of the aqueous phase, as well as on the vapor pressure of H_2O .

(8) T_NonDarcian_Flow.f95 (#)

Code unit that computes all parameters and variables needed for the application of non-Darcian flow through porous and fractured media by accounting for inertial (turbulent) or viscous (slippage) effects. Thus, this unit reads all the non-Darcian flow inputs, and then uses them to compute all the parameters of the turbulent flow options (*Forcheimer* [1901] or *Barre and Conway* [2007]), of slippage flow (Klinkenberg flow [*Klinkenberg*, 1941], Knudsen diffusion [*Freeman et al.*, 2011] or the Dusty Gas Model [*Mason and Malinauskas*, 1983; *Webb*, 1998]).

(9) T_Geomechanics.f95

Code unit that describes the geomechanically-induced changes on the flow properties of the porous media. These include porosity ϕ changes caused by pressure and/or temperature variations, intrinsic permeability k changes caused by porosity changes, and scaling of capillary pressures P_{cap} to reflect changes in ϕ and k. The ϕ and k changes are computed using either simplified of full geomechanical models. When the simplified model is invoked, ϕ is a function of (a) P and the pore compressibility α_P and (b) of Tand the pore thermal expansivity α_T , while (c) k changes are estimated using empirical relationships (see Section 8). Changes in ϕ and k can also be computed by using a full geomechanical model, which can be optionally coupled with TOUGH+.

(10) T_RealGasBrine_Specifics.f95 (*)

Code unit that includes procedures specific to the **T+RGB** simulation, such as the reading of T+RGB-specific inputs, the preparation of the case-specific output files, the computation of the maximum amount of gas dissolved in the aqueous phase in the presence of salt, the computation of the sorbed gas masses, etc.. Generic procedures and operator extension – which override (*overload*) the standard procedures used by TOUGH+ for the simulation of general problems – are defined in this code unit, which does not include any procedures describing the gas + H₂O + salt equation of state.

(11) T_Main.f95

Main program that organizes the calling sequence of the high-level events in the simulation process, and includes the writing of important general comments in the standard output files, timing procedures, and handling of files needed by the code and/or created during the code execution.

(12) T_RealGasBrine_EOS.f95 (*)

Code unit that describes all the equations of state of the system, assigns initial conditions, computes the flow and thermophysical properties of the fluids, computes the flow properties of the medium, and determines phase changes and the state of the system from the possible options (see Section 3.1). This code unit also includes the procedure that computes the elements of the Jacobian matrix for the Netwon-Raphson iteration.

(13) T_Matrix_Solvers.f95

A linear algebra package that includes all the direct and iterative solvers available in TOUGH+ (see *Moridis* [2014]).

(14) T_Executive.f95

The executive code unit of TOUGH+. It includes the procedures that advance the time in the simulation process, estimate the time-step size for optimum performance, populate the matrix arrays and invoke the solvers of the Jacobian, invoke special linear algebra for matrix pre-processing in cases of very demanding linear algebra problems, compute mass and energy balances, compute rates in sources and sinks, compute binary diffusion coefficients, write special output files, and conduct other miscellaneous operations.

(15) T Inputs.f95

This code unit includes the procedures involved in the reading of the general input files needed for TOUGH+ simulations. It does not include any procedure reading T+RGB-related data (this is accomplished in the **T_RealGasBrine_Specifics.f95** code unit).

The code units denoted by (*) are specific to the T+RGB problem. The code unit denoted by (#) is not part of core TOUGH+ code but of the wider supplemental TOUGH+ code ensemble [*Moridis*, 2014], and is invoked to carry out the computations related to the system behavior needed by the REALGASBRINE v1.0 application option. All other code units are common to all TOUGH+ simulations.

Additionally, **T**+ **RGB** is distributed with the **Meshmaker.f95** FORTRAN code, which used to be part of the main code in the TOUGH2 simulators [*Pruess et al.*, 1999], but is a separate entity in the TOUGH+ family of codes. **Meshmaker.f95** is used for the space discretization (gridding) of the domain of the problem under study (see *Moridis* [2014]).

NOTE: In compiling **T**+**RGB**, *it is important that the free-format source code option be invoked for proper compilation*.

4.0. Input Data Requirements

In this section, we discuss in detail mainly the input requirements that are specific to the needs of the REALGASBRINE v1.0 application option. All inputs that are generic in type and common to any simulation of flow and transport through porous media are fully described in *Moridis* [2014] and will not be repeated here. The reader is directed to the *Moridis* [2014] report for details on the description of all such inputs and on the structure of the input files. Note that, to ensure backward compatibility with input files from older simulations, some input data for **T+RGB** simulations conform to older formats. The data inputs to activate the new capabilities in TOUGH+ v1.5 and REALGASBRINE v1.0 follow more advanced formats such as namelists.

Some of these non-EOS specific data are also discussed here (in essence, repeating the information in *Moridis* [2014]) for additional emphasis, as these *may* play an important role in **T+RGB** simulations. Unless otherwise indicated, all input data are in standard

metric (SI) units, such as meters, seconds, kilograms, °C and in the corresponding derived units, such as Newtons, Joules, Pascal (= N/m^2 for pressure), etc.

4.1. Input Data Blocks

In the **T+RGB** input files, data are organized in standard TOUGH2 and TOUGH+ structure that involves data blocks that are defined by keywords. **Table 4.1** provides a listing and a short description of all the data blocks (mandatory and optional) in a **T+RGB** input file. Note that, as a result of the modular structure of the TOUGH+ architecture [*Moridis*, 2014], only a single data block (REAL_GAS+H2O or REAL_GAS+H2O) is specific to this application option, and all other ones are generic and common to any TOUGH+ simulation.

4.2. Data Block MEMORY

This block is a mandatory component of the generic TOUGH+ input file, and is discussed here only in order to provide a list of values for the parameters needed for an appropriate allocation of the dynamic memory. Thus, the following options are possible:

binary_diffusion	= . TRUE . if diffusion is considered
	=.FALSE. if diffusion is ignored

The following combinations are possible for **T+RGB** simulations:

(1)	(NumCom,	NumEq,	NumPhases)	$= (2, N_{g}+1, 2)$:
	Water,	, real gas n	nixture, no salt, is	sothermal

(2) (NumCom, NumEq, NumPhases) = (3, N_G+2, 2): Water, real gas mixture, no salt, non-isothermal

Keyword (+)	Sec. (#)	Function		
TITLE (1 st record)	4.1.1	Data record (single line) with simulation title		
MEMORY (2 nd record)	5.1	Dynamic memory allocation		
REAL_GAS+H2O or	4.2(^)	Parameters describing the case-specific T+RGB system		
REAL_GAS+Brine		properties		
ROCKS or MEDIA	6.2	Hydrogeologic parameters for various reservoir domains		
RPCAP or WETTABILITY	6.3	Optional; parameters for relative permeability and capillary pressure functions		
DIFFUSION	6.4	Optional; diffusivities of mass components		
*ELEME	7.1	List of grid blocks (volume elements)		
*CONNE	7.2	List of flow connections between grid blocks		
INDOM	8.1	Optional; initial conditions for specific reservoir domains		
*INCON	8.2	Optional; list of initial conditions for specific grid blocks		
EXT-INCON	8.3	Optional; list of initial conditions for specific grid blocks		
BOUNDARIES	8.6	Optional; provides time-variable conditions at specific boundaries		
*GENER	9.1	Optional; list of mass or heat sinks and sources		
PARAM	10.1	Computational parameters; time stepping and convergence parameters; program options		
SOLVR	10.2	Optional; specifies parameters used by linear equation solvers.		
TIMES	11.2	Optional; specification of times for generating printout		
SUBDOMAINS	11.3	Optional; specifies grid subdomains for desired time series data		
INTERFACES	11.4	Optional; specifies grid interfaces for desired time series data		
SS_GROUPS	11.5	Optional; specifies sink/source groups for desired time series data		
ENDCY (last record)	4.1.3	Record closes TOUGH+ input file and initiates simulation		
ENDFI (last record)	4.1.4	Alternative for closing TOUGH+ input file which causes flow simulation to be skipped.		

 Table 4.1. Input data blocks for T+RGB

#: Denotes the section number in the Moridis [2014] report

^: Denotes the section number in this report

*: Data can be provided as separate disk files and omitted from input file.

+: The bold face part of the keyword (left column) suffices for data block recognition

- (3) (NumCom, NumEq, NumPhases) = (3, N_g+2, 3): Water, real gas mixture, salt, isothermal
- (4) (NumCom, NumEq, NumPhases) = (4, N_g+3, 3): Water, real gas mixture, salt, non-isothermal

Any value of the NumCom, NumEq, NumPhases parameters other than those described here results in an error message and the cessation of the simulation. The selection of appropriate values for all other variables in this data block is left to the user.

4.3. Data Block ROCKS or MEDIA

The discussion here is limited to the specific parameters that may be needed in a T+RGB

simulation. Information on all the other parameters in the specified records is found in

Moridis [2014].

Record ROCKS.1

NAD = 8: In addition to the standard four records read for NAD > 2, an additional (fifth) record will be read with information on the whether slippage and inertial/turbulent flow effects will be considered in this medium.

Record ROCKS.1.4

Optional, for NAD = 8 only. This record includes general data describing whether non-Darcian flow is to be considered in this medium. The namelist in this record is named Slippage_Turbulence_Info, and has the following general form:

&Slippage Turbulence Info	MediumKnudsenFlow F	=	.x.,
	MediumTurbulentFlow_F	=	.x.,
	MediumKlinkFlow F	=	.x.,
	Option KlinkenbergParam	=	'x′
	/ = -		

The parameters in the namelist NonDarcian_Flow_Specifications are defined as follows:

MediumKnudsenFlow F

A logical parameter indicating whether Knudsen diffusion will be considered in this medium. The possible values are .TRUE. or .FALSE.

MediumTurbulentFlow F

A logical parameter indicating whether turbulent flow will be considered in this medium. The possible values are .TRUE. or .FALSE.

MediumKlinkFlow_F

A logical parameter indicating whether Klinkenberg flow (gas slippage) will be considered in this medium. The possible values are .TRUE. or .FALSE.

Option KlinkenbergParam

A character parameter of length LEN = 5 defining the method to be used for the estimation of the slippage parameter b. The following options are available:

= 'CON': The *b* value provided in the data block **ROCKS** (see *Moridis* [2014]) is used.

= 'FIXED': The *b* value is obtained as a function of the initial intrinsic permeability *k* from interpolation in a table provided by Wu et al. [1988] and remains fixed during the simulation (default).

= 'C-INT': The *b* value is obtained as a function of the **initial (constant)** k from interpolation in a table provided by *Wu et al.* [1988] and varies with k during the simulation.

= 'V-INT': The *b* value is obtained as a function of the **variable** k (changing during the simulation as a result of changing *P* and *T*) from interpolation in a table provided by *Wu et al.* [1988] and varies with *k* during the simulation.

= 'C-REF': The *b* value is obtained as a function of a reference **constant** *k* using the method of *Jones* [1972] and interpolation in a table provided by $Wu \ et \ al.$ [1988].

= 'V-REF': The *b* value is obtained as a function of a reference **variable** k (changing during the simulation as a result of changing *P* and *T*) using the method of *Jones* [1972] and interpolation in a table provided by *Wu et al.* [1988].

= 'C-JOW': The *b* value is obtained as a function of a reference **constant** (initial) k using the method of *Jones and Owens* [1979].

= V - JOW': The *b* value is obtained as a function of a reference **variable** *k* (changing during the simulation as a result of changing *P* and *T*) using the method of *Jones and Owens* [1979].

= 'C-SAK': The *b* value is obtained as a function of a reference **constant** (initial) *k* and ϕ using the method of *Sampath and Keighin* [1981].

= 'V-SAK': The *b* value is obtained as a function of a reference **variable** k (changing during the simulation as a result of changing *P* and *T*) and ϕ using the method of *Sampath and Keighin* [1981].

= 'C-FLO': The b value is obtained as a function of a reference **constant** (initial) k and b using the method of *Florence* [1988].

= 'V-FLO': The *b* value is obtained as a function of a reference **variable** k (changing during the simulation as a result of changing *P* and *T*) and ϕ using the method of *Florence* [1988].

4.3. Data Block REAL_GAS+H2O or REAL_GAS+Brine

The parameters describing the system properties and behavior are provided here. Note that namelist-based format is used to read the data in this data block. This is a very powerful format that allows maximum clarity and flexibility, accepting free formats, arbitrary ordering of variables, insertions of comments anywhere in the input fields, and providing the option of ignoring any of the NAMELIST parameters by not assigning a value to it. For more information, the reader is directed to a textbook on FORTRAN 95/2003.

Record TRGB.1

This record includes general data describing whether non-Darcian flow is to be considered. The namelist in this record is named NonDarcian Flow Specifications, and has the following general form:

```
&NonDarcian_Flow_Specifications
    turbulent_flow_F = .x.,
    turbulent_phase_flow_F = .x.,
    Option_turbulent_FlowEquation = 'x',
    Option_turbulent_FlowEqParam = 'x',
    Knudsen_diffusion_F = .x.,
    slippage_effects_F = .x.,
    dusty_gas_model_F = .x.,
    /
```

The parameters in the namelist NonDarcian_Flow_Specifications are defined as follows: turbulent flow F

A logical parameter indicating whether turbulent flow will be considered at all. The possible values are .TRUE. or .FALSE.

turbulent_phase_flow_F

A logical array of dimension NumMobPhases indicating whether flow of any of the mobile phases is turbulent flow. The possible values of each array element are .TRUE. (mainly for the gas phase) or .FALSE. (usually for the aqueous phase).

Option_turbulent_FlowEquation

A character parameter of length 5 defining the type of turbulent flow equation to be used. The following options are available:

= 'FORCH': This option invokes the *Forchheimer* [1901] equation for turbulent flow.

= 'BARCO': The *Barree and Conway* [2007] equation is used.

Option_turbulent_FlowEqParam

A character parameter of length 3 defining the method to compute the parameters for the chosen turbulent flow equation to be used. The following options are available:

= 'CON': A constant value is used for the parameter β_{FB} of the Forchheimer

[1901] equation for turbulent flow.

= 'LIU': This option invokes the *Forchheimer* [1901] equation for turbulent flow.

= 'G': The method of *Geertsma* [1974] is used (default).

= 'JK': The method of *Janicek and Katz* [1955] is used.

= 'FG3 ': The method of *Frederick and Graves* [1994], Eq. 3 is used.

= 'FG4 ': The method of *Frederick and Graves* [1994], Eq. 4 is used.

= 'FG5 ': The method of *Frederick and Graves* [1994], Eq. 5 is used.

= 'FG6': The method of *Frederick and Graves* [1994], Eq. 6 is used.

= 'LIU': The method of *Liu et al.* [1995] is used.

= 'TM': The method of *Thauvin and Mohanty* [1998] is used.

= 'CM': The method of *Coles and Hartman* [1998] is used.

= 'C': The method of *Cooper et al.* [1999] is used.

= 'E': The method of *Ergun* [1952] is used. Knudsen_diffusion_F A logical parameter indicating whether Knudsen diffusion will be considered at all. The possible values are .TRUE. or .FALSE.

```
slippage effects F
```

A logical parameter indicating whether slippage effects (Klinkenberg flow) will be considered at all. The possible values are .TRUE. or .FALSE.

```
dusty_gas_model_F
```

A logical parameter indicating whether the dusty gas model [*Webb*, 1998] will be considered at all. The possible values are .TRUE. or .FALSE.

Record TRGB.2

This record includes general data describing key diffusion parameters. The namelist in this record is named Gas_Specifications, and has the following general form:

```
&Gas_Specifications number_of_component_gases = x,
    component_gas_name ='x',..., 'x',
    component_gas_mole_fraction = x,...,x
    gas_cubic_EOS = 'x',
    sorbed_gas_F = .x.,
    variable_gas_composition_F = .x.
    /
```

The parameters in the namelist NonDarcian_Flow_Specifications are defined as follows:

number_of_component_gases

An integer parameter specifying the number of gases; water may be omitted, as it is automatically added by the code.

component_gas_name

A character array of length 6 and of dimension number_of_component_gases describing the names of the gases. The possible options are:

```
CH4, C2H6, C3H8, nC4H10, nC4H10, H2O, CO2, H2S, O2, N2, C2H5OH and H2
```

component_gas_mass_fraction

A real array of dimension number_of_component_gases describing the mole fractions of the gases in the initial gas mixture.

gas_cubic_EOS

A character parameter of length 3 defining the type of the cubic equation of state to be used for the gas mixture. The following options are available:

= ' PR ': This option invokes the *Peng and Robinson* [1976] equation for turbulent flow (default).

= 'SRK': The Soave [1972] equation is used.

= 'RK': The *Redlich and Kwong* [1949] equation is used.

sorbed_gas_F

A logical parameter indicating whether gas sorption will be considered at all. The possible values are . TRUE. or . FALSE.

variable gas composition F

A logical parameter indicating whether the dry gas will be treated as a constant-composition pseudo-component (=.FALSE.), or if its constituent gases will be tracked individually (=.TRUE.).

Record TRGB.3

This record is needed only if $sorbed_gas_F = .TRUE.$, is named Sorption_Specifications, its function is self-explanatory, and has the following general form:

&Gas_Specifications	medium_name	=	'x',
	medium_number	=	x,
	sorbing_comp_name	=	'x'
	sorbing_comp_number	=	x,
	sorption_equation_name	=	'x',
	sorption_parameters	=	x,,x
	/ _		

The parameters in the namelist NonDarcian_Flow_Specifications are defined as follows:

medium_name

A character parameter of length 5 specifying the name of the sorbing rock (see data block **ROCKS** in *Moridis* [2014]).

medium number

An integer parameter specifying the number of the sorbing rock in the listing sequence (see data block **ROCKS** in *Moridis* [2014]). Either the name or the number of the sorbing rock is sufficient.

sorbing_comp_name

A character parameter of length 6 specifying the name of the sorbing gas component (see record TRGB. 2 above).

sorbing_comp_number

An integer parameter specifying the number of the number of the sorbing in the listing sequence (see record TRGB. 2 above).

component_gas_name

A character array of length 6 and of dimension

number_of_component_gases describing the names of the gases. The possible options are: CH4, C2H6, C3H8, nC4H10, nC4H10, H2O, CO2, H2S, O2, N2, C2H5OH and H2

component_gas_mass_fraction

A real array of dimension number_of_component_gases describing the mole fractions of the gases in the initial gas mixture.

sorption_equation_name

A character parameter of length 10 specifying the name of the sorption equation for the specified rock and spesies. The options are:

= 'EQU-LANG-B' or 'EQU-LANG-B': Equilibrium Langmuir sorption

= 'KLAS ': Kinetic Langmuir sorption

= 'ELIS': Equilibrium linear sorption

= 'KLIS': Kinetic linear sorption.

= 'EFS ': Equilibrium Freundlich sorption

= 'KFS': Kinetic Freundlich sorption.

sorption parameters

A real array of dimension 6 listing the parameters of the sorption equation.

Record TRGB.4

This record is needed only if the data block name is **REAL_GAS+BRINE**, is named Brine_Specifications, its function is self-explanatory, and has the following general form:

The parameters in the namelist Brine_Specifications are defined as follows:

brine_viscosity_computation_method

A character parameter of length 3 specifying the method to compute the brine viscosity. The possible options are:

= 'MAO': The method of *Mao and Duan* [2009]

= ' PHI ': The method of *Phillips et al.* [1981]

brine_enthaly_computation_method

A character parameter of length 3 specifying the method to compute the brine enthalpy. The possible options are:

- = 'LOR': The method of *Lorenz* [2000]
- = 'MIC': The method of *Michaelides* [1981]
- = 'MIL': The method of *Miller* [1978]

4.5. Data Block DIFFUSION

This block reads multicomponent diffusion coefficients using a NAMELIST format. This is a very powerful format that allows maximum clarity and flexibility, accepting free formats, arbitrary ordering of variables, insertions of comments anywhere in the input fields, and providing the option of ignoring any of the NAMELIST parameters by not assigning a value to it. For more information, the reader is directed to a textbook on FORTRAN 95/2003.

In **T+RGB** applications, this capability may be invoked in long-term studies (covering multi-year periods). Diffusion is not expected to play a significant role in the course of most cases of production from gas-bearing geologic media because, in such a case, advective effects constistently overwhelm diffusive transport.

Record DIFFUSION.1

This record includes general data describing key diffusion parameters. The namelist in this record is named Diffusion_Key_Parameters, and has the following general form.

&Diffusion_Key_Parameters
 gas_diffusivity_equation_exponent = x.xEx,
 P_at_RefDiffusivity = x.xEx,
 Tk_at_RefDiffusivity = x.xEx
 full_multiphase_diffusion = .x
 /

The parameters in the namelist Diffusion_Key_Parameters are defined as follows:

gas diffusivity equation exponent

A double precision variable describing the dependence of gas diffusivity on temperature (see Equation 6.4 in *Moridis* [2014]). The default value is 1.80.

P at RefDiffusivity

Pressure at the reference diffusivity (in Pa). If $P_at_RefDiffusivity <= 0$, the default value is 10^5 Pa.

Tk_at_RefDiffusivity

Temperature at the reference diffusivity (in K). If

T_at_RefDiffusivity <= 0, the default value is 273.15 K.

Option_gas_diffusivity_CompuMethod

A character variable describing the method of estimation of the binary **gas** diffusivities. The following options are available:

= 'Standard': This option involves the application of Equation (6.4) in *Moridis* [2014], and requires non-zero multicomponent gas diffusivity values read from the standard input file.

= 'Real_Gas_EOS': In this case, the binary gas diffusivities are computed from the cubic equation of state used to determine all the real gas properties. The diffusivities in the aqueous phase still need to be provided.

= 'Constant': When this option is invoked, the constant multicomponent diffusivity values provided in the input file are used.

full multiphase diffusion

A logical variable describing the method of estimation of the method of estimation of multiphase diffusive fluxes. The following options are available:

= . TRUE . : With this option, harmonic weighting to the full multiphase effective diffusion strength is applied. This includes contributions from gas and aqueous phases, accounts for coupling of diffusion with phase partitioning effects, and can describe the most general cases of diffusion across phase boundaries.

= . FALSE .: In this case, harmonic weighting is performed separately for the diffusive fluxes in the mobile phases.

Records DIFFUSION.2.1, DIFFUSION.2.2, etc.

Record <u>DIFFUSION.2.1</u> is followed by DIFFUSION.2.x records, with x = 1, ..., NubMobPhases (i.e., the number of mobile phases in the system under study). These records describe component diffusivities in the various phases. The same namelist is used in each one of these records. It is named Component_Diffusivities_in_Phases, and has the following general form:

```
&Component_Diffusivities_in_Phases
    phase = x,
    phase_number = x,
    component(1) = x,
        component_number(1) = x,
        component_diffusivity(1) = x.xEx,
        component(2) = x,
        component_number(2) = x,
        component_diffusivity(2) = x.xEx,
    ...
    ...
    ...
    ...
    ...
    ...
    //
```

The parameters in the namelist Diffusion_Key_Parameters are defined as follows:

phase

A character variable identifying the mobile phase for which the diffusivities of the various components are reported. The possible options in the **T+RGB** code are 'Aqueous' and 'Gas'.

```
phase_number
```

An integer variable providing the number of the phase in the phase numbering sequence used in the code. The possible options in the **T+RGB** code are:

- = 2 for phase = 'Aqueous', and
- = 1 for phase = 'Gas'.

component

A character array of dimension NumCom (see Section 5.1) identifying the various mass components particle in the phase in question (denoted by phase). The possible options in the **T+RGB** code are 'CH4', 'H2O' and 'NaCl' (if salinity is considered).

component_number

An integer array providing the number of the component in the numbering sequence used in the code. The possible options in the **T**+**RGB** code are:

- = 1 for component = 'CH4'
- = 2 for component = 'H2O'
- = 3 for component = 'NaCl' (if present)

component diffusivity

A double precision array of dimension NumCom (see Section 5.1) describing the value of the multicomponent diffusivities D_{β}^{κ} (see Equations (2.59) and (6.4)) of the various components κ in the phase β under consideration (indentified by phase and phase_number, respectively).

NOTE: The records DIFFUSION.2.x must provide data for all mobile phases and all components, even if the gas diffusivities may be overridden internally when Option_gas_diffusivity_CompuMethod = 'Real_Gas_EOS'.

The structure of the namelists Diffusion_Key_Parameters and Component_Diffusivities_in_Phases (and their use as input formats in the data block **DIFFUSION**) are best illustrated in the example of **Figure 4.1**.

DIFFUSION*2*3*4*5*6*7*8
&Diffusion Key Parameters gas diffusivity equation exponent = 1.8d0
P at RefDiffusivity = 1.0d5, ! in Pa
$T\overline{K}$ at RefDiffusivity = 273.15d0, ! in K
Option gas diffusivity CompuMethod = 'Real Gas EOS'.
full multiphase diffusion = .TRUE.
Component Diffusivities in Phases
$h_{2} = h_{2} = -\frac{1}{2} m_{2} = h_{2} = h_{$
$f_{\text{phase}} = A_{\text{phase}} = A_{p$
component (i) = (cha), component (i) = 1,
Component diffusivity(1) = 1.00-10, 1 (m2/s) (Diffusivity of component 1 in phase 2
$\operatorname{component}(2) = \operatorname{H2O}(2)$, $\operatorname{component}(2) = 2$,
component diffusivity $(2) = 1.0d-10$, $! (m2/s) ! Diffusivity of component 2 in phase 2$
component(3) = 'NaCl', component_number(3) = 3,
component_diffusivity(3) = 1.0d-10 ! (m2/s) ! Diffusivity of component 3 in phase 2
&Component_Diffusivities_in_Phases
phase = 'Gas', phase number = 1,
component(1) = 'CH4', component number(1) = 1,
component diffusivity(1) = $1.0d-05$, [(m2/s) ! Diffusivity of component 1 in phase 1
component(2) = 'H2O', component number(2) = 2.
component diffusivity(2) = $1.0d-05$. $1.(m2/s)$ Diffusivity of component 2 in phase 1
component(3) = NaCl' component number(3) = 3
component diffusivity(3) = 0.0d-00 $-1.002/s$ Diffusivity of component 3 in phase 1
/ / / / / / / / / / / / / / / / / / /

Figure 4.1. The DIFFUSION data block, with examples of the Diffusion_Key_Parameters and Component Diffusivities in Phases namelists

5. Outputs

In this section, the various primary and secondary variables that may be provided as outputs from T+RGB simulations are discussed. Such outputs are provided in the following cases:

- In the standard T+RGB output as an ASCII file either at selected times (defined in the data blocks TIMES), or at a given timestep frequency (defined by the variable PRINT_frequency in the data block PARAM, see *Moridis* [2014]). The standard output provides information on all elements and connections in the grid of the system.
- In an output file named Plot_Data_Elem, which stores the element-specific properties and parameters in a format that conforms to the requirements of the TecPlot package [*TecPlot*, 2003], and is suitable for most other plotting and graphing packages. This file is printed when the variable MOP(19)=8 for 9 in the

data block PARAM and provides information on all elements of the domain (see *Moridis* [2014]). Note that for MOP(19) = 9, the plotting file and a truncated standard output file are produced (listing only mass balances at the prescribed printout times).

 In output files named after each of the subdomains, interfaces or groups of sinks and sources (wells) defined in the data blocks SUBDOMAINS, INTERFACES and SS_GROUPS, respectively. These files provide time series of relevant data at a frequency determined by the input parameter TimeSeries_frequency in the in the data block PARAM (see *Moridis* [2014]).

5.1. The Standard Outputs

The standard output of the **T**+**RGB** code provides the following output:

- 1. The pressure, temperature, phase saturations, gas partial pressure, H_2O vapor pressure, sorbed gas mass and salt mass fraction in all elements of the domain.
- 2. The mass fractions of the individual gases in the gas and aqueous phases, phase densities and viscosities, porosities, capillary pressure and relative permeabilities to the mobile phases.
- 3. The flows and velocities of the phases through the element interfaces (connections) of the domain; the corresponding flows of the gas constituents in the mobile phases (i.e., aqueous and gas), and the heat flow; the diffusive flows (if accounting for diffusion).
- 4. The primary variables and their changes in the elements of the domain.
- 5. The phase enthalpies, the temperature shift (when salt is present), the intrinsic permeabilities and the permeability-reduction factor in the presence of solid phases (if the EPM model is used, see *Moridis* [2014]) in all elements of the domain.
- 6. Source and sink (well) information, including: mass and enthalpy rates, mobile phase mass fractions in the injection/production stream, gas and H_2O mass flow rates in the mobile phases.

7. Volume and mass balances of the phases and components in the domain.

All the units of the various parameters are listed in the standard output file. Of the possible outputs, (1), (2), (6) and (7) are always printed in the standard **T+RGB** output. The amount of the additional output is controlled by the parameter OutputOption in the data block PARAM. Thus, (3) is printed in addition when OutputOption = 2, and a complete data set (items 1 to 7) is printed when OutputOption = 3. In keeping with the TOUGH2 [Pruess et al., 1999] and TOUGH + convention [*Moridis*, 2014], printouts occur after each iteration (not just after convergence) if the OutputOption values are increased by 10.

For MOP (19) >7, the **Plot_Data_Elem** file includes the following information: the coordinates of each element center in the domain, and the corresponding pressure, temperature, phase saturations, relative permeability of the mobile (aqueous and gas) phases, the capillary pressure, the component (gases, H₂O and salt) mass fractions in the various phases, the sorbed gas mass, permeability, porosity and the permeability-reduction factor in the presence of solid phases (meaningful only if the EPM model is invoked, see *Moridis* [2014]).

5.2. Time Series Outputs

Time series outputs are obtained when the data blocks SUBDOMAINS, INTERFACES and SS_GROUPS are included in the **T+RGB** input files. Thus, individual output files are created for each one of the subdomains identified in SUBDOMAINS (see detailed discussion

in *Moridis* [2014]), and there the following data are written with a frequency defined by the parameter TimeSeries_frequency:

- The subdomain pore volume, and pore-volume averaged pressure, temperature, and gas saturation in the subdomain.
- The mass of each of the phases and of the salt (if present).
- The mass of the individual gases in the aqueous and the gas phase, and on the grains of the porous medium (sorbed).

Similarly, individual output files are created for each one of (a) the interfaces identified in SUBDOMAINS and (b) the source/sink (well) groups identified in SS_GROUPS (see detailed discussion in *Moridis* [2014]), and there the following data are written with a frequency defined by the parameter TimeSeries_frequency:

- The mass flow rate of the mobile (aqueous and gas) phases across the interface or through the source/sink group, as well as the corresponding individual gas and H₂O flows in each of the mobile phases, the salt flow and the heat flow.
- The cumulative mass of each of the mobile (aqueous and gas) phases that flowed across the interface or through the source/sink group since the beginning of the simulation, as well as the corresponding mass of individual gas and H₂O in each of the mobile phases and the salt mass.

All the units (SI) of the various listed parameters are listed in the headings of the output file.

6.0. Example Problems

6.1. Example Files and Naming Conventions

The files corresponding to the examples discussed in this manual can be found in the directory Test_Problems_TRBG_V1.0 in the USB memory stick accompanying this manual. The input files of the example problems are the following:

- 1. Test1
- 2. Test2
- 3. Test3
- 4. Test4
- 5. Test5
- 6. ProblemV1
- 7. ProblemV2
- 8. ProblemV3
- 9. ProblemA1

Of those, the ones with the 'ProblemV' identifier are used to demonstrate the range of capabilities of the code. Those with the 'ProblemV' identifier denote problems

of validation of existing analytical solutions, and those with the 'ProblemA' identifier denote larger application problems.

output files The corresponding are also included in the directory "Test Problems TRBG V1.0" on the memory stick distributed during the class. The naming convention of the generic TOUGH+ output files involves the suffix ".out" at the end of the input file name. For the case of **Test1**, some additional files that are created per the specifications of the output options in the input data files are also included. These have the user-defined names 'WellZ Time Series', 'IntRR Time Series' and 'Wells Time Series' and (see input file Test1 in the Appendix or on the memory stick), and represent time series of data at subdomain, through an interface and through a source/sink group, respectively.

6.2. Problem Test1: Single Gas Flow and H2O, Radial System, Gas, Non-Isothermal

This 1-D radial problem is designed to demonstrate the basic concepts of input file creation and structure, and to demonstrate the evolution of the state of a cylindrical reservoir in the course of production. The gas is 100% CH₄, there is no salt in the system, and the reservoir is initially at a 2-phase state with $S_A = 0.5$. This is a low-permeability system tight-sand system, which means that gas sorption onto the grains of the porous medium can is minimal and can be ignored. The simulation accounts for Knudsen diffusion, the parameters of which are computed internally using the equations discussed in Section 2. As production continues, the pressure is expected to continuously decline, and the same is expected of the temperature because of the Joule-Thomson effect near the wellbore. Additionally, the pressure drop should also result in an increase in the apparent permeability of the system because of the increase in the mean travel path of the gas. Because all the physics are represented into the T+RGB code, this is expected to be a dynamic system, with all the fluid properties varying continuously.

For convenience, the input file is listed in **Figure 6.1**. As an exercise, a novice user is urged to identify the various variables and parameters in the input file.

The cylindrical domain (represented by 33 active cells of non-uniform radial increments and having a thickness of $\Delta z = 10$ m size) is a pressurized and thermally insulated reservoir of a porous medium, in which CH₄ and water coexist at a pressure of 10^7 Pa and T = 10 °C. At a time t = 0, production begins at three sinks (wells), one of which is located at the center of the cylindrical reservoir. The production rate is the same Q = 0.1 kg/sin all 3 wells. Note that, in a cylindrical system as the one described here (also known as single-well problems), it is next to impossible to have wells away from the center of the domain representing any real-life scenario, unless a large number of wells are installed on a circular pattern around the center well. However, here this is acceptable as a numerical exercise.

The porous medium has a porosity $\phi = 0.1$, and a permeability $k = 3 \times 10^{-15} \text{ m}^2$ (= 3 mD in oilfield units). Strictly speaking, this is not classified as a tight system, but this is not a problem because this sample problem is used for illustration purposes, and the permeability will be changed (and the problem rerun) during the training session. A non-zero pore compressibility (=10⁻⁹ 1/Pa, i.e., typical of sandstones) is assigned to the porous medium. This is necessary in hydrate simulations, in which evolution of solid phases of lower density (such as ice and hydrate) can lead to extraordinarily high pressures as the

aqueous phase disappears if pore compressibility is small. The thermal conductivity (=3.1 W/m/K) is also typical of water-saturated sandstone media. The relative permeability is computed from the Modified Stone equation, and the relative permeability from the vanGenuchten equation (see *Moridis* [2014])

Test1.out, the standard TOUGH+ output corresponding to the input file Test 1T, can be found in the directory Test Problems TRBG V1.0 in the USB memory stick accompanying this manual. Because MOP(5) = 0, the output does not includes detailed messages about the evolution of the residuals during the Newtonian iterations at each time step (phase changes are not possible in this system). Because OutputOption = 3, a full output is obtained that provides a very detailed list of the conditions, parameters and thermophysical properties of the system at each cell and at each connection. Thus, the output describes the pressure, temperature, phase saturation, partial CH₄, H₂O-vapor pressure, equilibrium hydration pressure, salt mass fraction in the aqueous phase, CH_4 concentrations in the aqueous and gas phases, phase densities, porosity, capillary pressure, relative permeability of the gas and aqueous phases, the amount of sorbed gas, heat and fluid fluxes, mobile phase velocities, CH₄ fluxes in the aqueous and gas phases, primary variables and their changes, phase enthalpies, the effect of Knudsen diffusion on the permeability, and the temperature shift in the hydrate P-T equilibrium caused by the presence of the inhibitor. Additionally, the output provides mass and volume balances of the phases, component mass balances, and component distribution into the phases.

The results in the portion of the output in the **Test_1T.out** file (see Appendix A) are consistent with the expected system response. Production at the central well caused the

pressure to drop, leading to an increase in the gas saturation (as more gas comes out of solution) and a temperature drop that increases over time because of Joule-Thomson cooling. The minimum pressure is observed at the production well; the two additional wells have practically no impact (as expected) because of the very large volume of the elements in which they occur and their low production rates. As expected, the water and gas flows indicate fluid movement toward the central production well. Note that, because of the location of the two wells away from the center, flow toward these wells from both directions is also observed.

The additional output files `WellZ_Time_Series', `IntRR_Time_Series' and `Wells_Time_Series' and (see input file Test1 in the Appendix or on the memory stick) have the user-defined names specified in Test1 and represent time series of data at a subdomain, through an interface and through a source/sink group, respectively. The data in each one of these files are clearly identified and their units are specified. In a continuation run (to be attempted during the training session), these files need to remain in the directory of the T+RGB execution because they provide vital information. The T+RGB code reads the last line of the data in each file, and uses some of these data in order to seamlessly continue the computation of the cumulative quantities of parameters of interest.

6.3. Problem Test2

This problem is a variation of that in **Test1**, from which it differs in the following aspects:

- Salt is now considered
- Klinkenberg effects are included
- Gas sorption is included
- Diffusion is included
- It has a single well at the center of the cylindrical reservoir

The reader is encouraged to (a) identify the data in the input file that enable these additional features, (b) run the **Test2** problem, and (c) compare the results to those from the run(s) in **Test1**. One of the important observations from the results of this simulation is the evolution of a solid phase because of the precipitation of salt as halite.

6.4. Problem Test3

This problem is another variation of that in **Test1**, from which it differs in the following aspects:

- o Salt is now considered
- Klinkenberg effects are included
- The dry gas is composed of two gases (CH_4 and C_2H_6), and these are treated as a pseudo-component of invariable composition during the simulation
- Gas sorption is included
- The initial conditions are now single-phase (aqueous), with dissolved gas
- It has a single well at the center of the cylindrical reservoir

As before, the novice **T**+**RGB** user is encouraged to (a) identify the data in the input file that enable these additional features of this illustrative example, (b) run the **Test3** problem, and (c) compare the results to those from the run(s) in **Test1**. One of the important observations from the results of this simulation is the evolution of a gas phase because of gas exsolution and salting out.

6.5. Problems Test4 and Test5

This problem is another variation of that in **Test1**, from which it differs in the following aspects:

- o Salt is now considered
- Klinkenberg effects are included
- The dry gas is composed of two gases (CH_4 and C_2H_6) in **Test4** and 4 gases in **Test5**, and these are treated as individual components, i.e., they are tracked independently
- Gas sorption is included
- The initial conditions are now single-phase (aqueous), with dissolved gas
- It has a single well at the center of the cylindrical reservoir

As before, the novice **T**+**RGB** user is encouraged to (a) identify the data in the input file that enable these additional features of this illustrative example, (b) run the **Test4** and **Test5** problems, (c) compare the results to those from the run(s) in **Test1**, and (d) run variations of these problems by modifying several inputs to determine the sensitivity of the results to these parameters and to the various computational options available in the code. One of the important observations from the results of these two simulations is the evolution of a gas phase because of gas exsolution and salting out.

6.6. ProblemV1: Real gas transient flow in a cylindrical reservoir

Using the concept of pseudo-pressure, *Fraim and Wattenbarger* [1986] developed a solution to the problem of transient flow in a finite cylindrical real-gas reservoir with a producing vertical well at its center, described as:

$$p_D = \frac{1}{2} E_i \left(\frac{r_D^2}{4t_D} \right) \tag{6.1}$$

where E_i denotes the exponential integral,

$$p_{D} = \frac{kh}{q_{V}B\mu}(\psi_{0} - \psi), \quad r_{D} = \frac{r}{r_{w}}, \quad t_{D} = \frac{k}{\phi\mu c_{t}r_{w}^{2}}t, \quad \psi = 2\int_{p_{r}}^{p}\frac{p}{\mu z}dp, \quad (6.2)$$

 ψ is the pseudo-pressure, r is the radius, r_w is the well radius [m], p is the pressure [Pa], p_r is a reference pressure [Pa], c_t is the total compressibility [Pa⁻¹], q_V is the volumetric production rate [ST m³/s], B is the formation volume factor, and h is the reservoir thickness. The subscript θ indicates initial conditions, and the subscript D denotes dimensionless variables.

The data used in the simulation of this validation problem appear in **Table 6.1.** The input files are provided in the directory Test_Problems_TRBG_V1.0 in the USB memory stick accompanying this manual. The gas was 100% CH₄. The cylindrical domain discretization involved a single layer, and a total of 32 logarithmically increasing Δr 's. **Figure 6.1** shows a very good agreement of the analytical and the **T+RGB** numerical

solutions at various sampling times. The \mathbf{T} + \mathbf{RGB} code yields an identical solution. Note that the problem was solved both isothermally and non-isothermally, and the difference between the two solutions was very small and localized in the vicinity of the well. This difference is attributed to Joule-Thomson cooling effects because of the bigger pressure drops and the high gas velocity at this location.

Data Type	Values
Matrix permeability k	$3.04 \text{x} 10^{-14} \text{ m}^2 (30.4 \text{ mD})$
Reservoir thickness h	10 m
Well radius r_w	0.059 m
Reservoir radius r_e	100 m
Reservoir pressure p	10 MPa
Reservoir temperature T	60 °C
Reservoir porosity ϕ	0.30
Rock compressibility	$2x10^{-10}$ 1/Pa
Gas composition	100% CH ₄
Gas EOS	Peng-Robinson

Table 6.11 — Properties and conditions in Problem V1.



Figure 6.1. Validation of the T+RGB code against the analytical solution of *Fraim and Wattenbarger* [1987] in Problem V1 of real gas transient flow in a cylindrical reservoir.

6.7. ProblemV2: Non-Darcy (Klinkenberg) Gas Flow

The *Klinkenberg* [1941] correction was originally developed to correct for the effect of gas slippage phenomena on permeability measurements of tight core samples. Depending on the flow rate, unconventional shale gas and tight gas sands may exhibit slip flow, or "Klinkenberg flow," in the reservoir itself. In order to correctly capture flow through such very low permeability media, the flow equations are derived in such a way that permeability is treated as a function of pressure that deviates from the theoretical permeability at infinite gas pressure according to $k = k_0(1+b/P)$.

As discussed earlier, there are several options for the computation of the Klinkenberg parameter *b* in **T+RGB**, see Section 4. *Wu et al.* [1988] used the pressure function $P_k = P + b$ to derived the following analytical solution to the problem of gas flow through an infinite cylindrical reservoir produced at a constant rate *q*:

The input parameters used in this problem are listed in **Table 6.2**. The input files are provided in the directory Test_Problems_TRBG_V1.0 in the USB memory stick accompanying this manual. The gas was 100% CH₄. The cylindrical mesh used in the **T+RGB** simulations involved a single layer and comprised 31 elements with logarithmically distributed Δr sizes. The agreement between the *Wu at al.* [1988] and the **T+RGB** solutions is excellent, as **Figure 6.2** clearly indicates. Additionally, given the short duration of the simulated period, the differences between the numerical predictions for isothermal and non-isothermal flow were practically negligible.


Table 6.2. Parameters in Problem V4 of Klinkenberg flow

Figure 6.2. Validation of the T+G code against the analytical solution of *Wu et al.* [1988] in ProblemV2 of Klinkenberg flow in a cylindrical gas reservoir.

6.8. Problem V3: Flow Into a Vertical Fracture With a Well at its Center

The solution of *Cinco-Ley and Meng* [1988] describes flow from a rectangular reservoir into a finite-conductivity vertical fracture intersected by a well at its center. The single biwing vertical fracture is a stimulation treatment typically applied to vertical wells in lowpermeability reservoirs. This complicated model transitions between two flow regimes over time. Bi-linear flow, where the dominant flow is through and perpendicular to the fracture face, is assumed at early times. At later times, the regime transitions into pseudo-radial flow.

The *Cinco-Ley and Meng* [1988] solution assumes flow for a slightly compressible liquid. In our computations, we used water as the reservoir fluid. The input files are provided in the directory Test_Problems_TRBG_V1.0 in the USB memory stick accompanying this manual. The properties and conditions used in the computations of two cases (differing only in the fracture permeability) in this problem are listed in **Table 6.3**. The Cartesian domain in the T+GW study involved a single layer, and was discretized into 60x60x1 = 3400 elements in (x,y,z). The comparisons in **Figure 6.3** between the analytical and the **T+RGB** solutions in the two cases (involving different values of $F_{CD} = k_f b_{f'}(k_m x_f)$, as k_f was different) show a very good agreement.

Case	p_i	k_m	k_f	h	q	B	μ	ϕ_m	C_t	x_f	F_{cD}	b_f
	kPa	$\Box m^2$	$\Box m^2$	m	m ³ /d		Pa.s		1/Pa	m		m
1	1.0E5	3.3E-3	3.0E3	10	172.8	1	4.91E-4	0.3	3.37E-10	20	10^{3}	0.022
2	1.0E5	3.3E-4	3.0E3	10	172.8	1	4.91E-4	0.3	3.37E-10	20	10^{4}	0.022

Table 6.3. Properties and conditions in Problem V5



Figure 6.3. Validation of the T+RGB code against the analytical solutions of *Cinco-Ley and Meng* [1988] in ProblemV3 of flow into a vertical fracture intersected by a vertical well at its center. Case 1: F_{CD} = 10; Case 2: F_{CD} = 10⁴.

6.9. ProblemA1: Gas Production From a Shale Gas Reservoir Using a Horizontal Well

This **T+RGB** study focuses on a Cartesian 3D stencil of a horizontal well section that is typical of a Type I shale gas system (**Figure 6.4**), as defined and investigated by *Freeman* [2010] and *Moridis et al.* [2010]. Such systems involve the (usually hydraulically) induced primary fractures (PF), the undisturbed matrix, and the stress release fractures around the well. The data used in this simulation were as in *Freeman* [2010]. The surface area of the Cartesian system at the well was corrected to reflect its cylindrical geometry. The simulated 3D domain (**Figure 6.4**) represents the stencil of the horizontal well system, i.e., the smallest repeatable subdomain that can accurately describe the system behavior. Studies by *Olorode* [2011] and [2012] have confirmed that such stencils are accurate representatives of the behavior of the entire system for very long production periods.

The discretization of the 3D domain involved subdivisions as small as mm-scale near the fracture face, and resulted in about 800,000 gridblocks. To develop the mesh file, we used an expanded version of the MESHMAKER facility available to the TOUGH+ code [*Moridis*, 2014] and its MINC option [*Pruess*, 1983], in addition to a short FORTRAN code written for this purpose. Two different media were considered: the matrix and the hydraulically induced fracture, which was represented by appropriate flow and thermal properties. The problem was solved both isothermally and non-isothermally. The gas was 100% CH₄, and its sorption onto the shale followed an equilibrium Langmuir isotherm.

Using the **T+RGB** code and assuming isothermal conditions, the predicted production rate when the well is operated at a constant bottomhole pressure P_w is shown in **Figure 6.5**, which also lists the data used in the simulation. Here we employ the the dimensionless variables commonly used in such studies, which are defined as:

$$t_{D} = \frac{k}{\varphi \mu c_{t} x_{f}^{2}} \frac{1}{[1 + V_{L}]} t, \ q_{D} = \frac{B \mu}{k h(p_{i} - p_{wf})} q,$$
(6.4)

$$q_{Di}(t) = \frac{1}{t} \int_{0}^{t} q_{D}(\tau) d\tau, \text{ and } q_{Did}(t) = -t \frac{dq_{Di}}{dt}$$
(6.5)

Figure 6.6 shows the distribution of the normalized pressure in the vicinity of the fracture face on the (x,y) plane along the length of the fracture at a height of 4 m above the well plane. Note the steep pressure gradients perpendicular to the fracture face that are the result of the very low permeability of the shale.



Figure 6.4. Stencil of a Type I system involving a horizontal well in a tight- or shale-gas reservoir [*Moridis et al.*, 2010].



Figure 6.5. Prediction of gas production in ProblemA1 [Freeman et al., 2010].



Figure 6.6. Pressure distribution in the vicinity of the hydraulically induced fracture in the shale gas system of ProblemA1 [*Freeman*, 2010]. Note the steep pressure gradient caused by the very low permeability of the shale.

7.0 Acknowledgements

The research described in this article has been funded by the U.S. Environmental Protection Agency through Interagency Agreement (DW-89-92235901-C) to the Lawrence Berkeley National Laboratory, and by the Research Partnership to Secure Energy for America (RPSEA - Contract No. 08122-45) through the Ultra-Deepwater and Unconventional Natural Gas and Other Petroleum Resources Research and Development Program as authorized by the US Energy Policy Act (EPAct) of 2005. The views expressed in this article are those of the author(s) and do not necessarily reflect the views or policies of the EPA. PAGE LEFT INTENTIONALLY BLANK

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APPENDIX

A Sample Input File

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```
<Test>: Gas production from a cylindrical gas (= CH4)+H2O reservoir
MEMORY
'REAL GAS+H2O'
   2
         3
             2 .FALSE.
                                               ! NumCom, NumEq, NumPhases, binary diffusion
'Cylindrical'
                35
                     90
                            5 .FALSE. .FALSE. ! coordinate system, Max NumElem, Max NumConx, ElemNameLength, active conx only, bou
   2
                                               ! MaxNum SS
   2
                                               ! MaxNum Media
                           'Saturation'
.FALSE.
         .TRUE. .FALSE.
                                               ! eleme by elem propert, poro perm depend, scaled cap pres, Option tortu CompuMethod
         'Continuous'
.FALSE.
                                               ! coupled geochemistry, property update = 'Continuous', 'Iteration', 'Timestep'
                'Continuous' 0
.FALSE.
         'XXX'
                                               ! coupled geomechanics, geomechanical code name, property update, num geomech param
ROCKS----1----*----2----*----3----*----4----*----6----*----7----*----8----*----9----*---10
DTRT1
               2.6e3
                            .10 3.00E-15 3.00E-15 3.00E-15
                                                                     3.1
                                                                             1000.
                                                                                      0.0d00
                                                                                                 3.0d-9
         8
                         0.50e0 0.00E+00 1.00E+05
                                                                  5.0e-2
                                                                             3.0e0
     1.e-9
                                                                                        0.0e0
                                                                                                  1.5e1
    9
                .150
                            .01
                                       4.
    7
             0.45000
                       1.49e-1
                                  5.0E-04
                                               1.E6
                                                        1.0e0
&Slippage Turbulence Info MediumKnudsenFlow F = .T., MediumTurbulentFlow F = .F.,
                            MediumKlinkFlow F = .F., Option KlinkenbergParam = 'FIX', Klink DirectionIndex = 1
                            1
BOUND
         0
               2.6e3
                         0.0e0 0.00E-13 0.00E-13 0.00E-13
                                                                   1.0e2
                                                                             1000.
REAL GAS+BRINE*----2----*----3----*----4-----*----5----*----6----*----8
&NonDarcian Flow Specifications
                                  turbulent flow F
                                                       = .FALSE.,
                                   Knudsen diffusion F = .TRUE.,
                                   slippage effects F = .FALSE.
&Gas Specifications number of component gases
                                                  = 1,
                                                  = 'CH4', 11*' ',
                     component gas name
                     component gas mole fraction = 1.0d0, 11*0.0d0
                     gas cubic EOS = 'PR',
                     sorbed gas F = .FALSE.,
                     variable gas composition F = .TRUE.
                      1
<<<
START----1----*----2----*----3-----*----4-----*----5-----*----6-----*-----8
----*---1 MOP: 123456789*123456789*1234 ---*---5----*---6----*----8
```

PARAM1-	*2	*3_	*4-	*5-	*6	*7	-*8-	*9	*10	*11
3 020	010100000	090000100	500003000	0.00E-5		0	10			
9	.83764E13	1.0e00	8.64E11		9.8060					
1.E-5	1.E00				1.0e-8	A	qG	1.0e-5	1.0e-5	1.0e-4
	1.000e7		5.00e-1		10.0e0					
SOLVR1-	*2	*3_	*4-	*5-	*6	*7	-*8			
3 Z1 O0	1.0e-2	1.0e-8								
ELEME	33 4	0 30	0.00000	500.100						
A00 0	17.	8540E-021	.5708E-02	0	.0000E+00	-5.	000E+00			
A00 1	17.	5398E-021	.5080E-02	5	.9161E-02	-5.	000E+00			
A00 2	15.	9133E-011	.1827E-01	1	.0383E-01	-5.	000E+00			
A00 3	11.	2955E+002	.5911E-01	1	.9813E-01	-5.	000E+00			
A00 4	12.	3990E+004	.7979E-01	3	.0954E-01	-5.	000E+00			
A00 5	14.	0954E+008	.1908E-01	4	.4266E-01	-5.	000E+00			
A00 6	16.	6675E+001	.3335E+00	6	.0216E-01	-5.	000E+00			
A00 7	11.	0527E+012	.1054E+00	7	.9344E-01	-5.	000E+00			
A00 8	11.	6272E+013	.2544E+00	1	.0229E+00	-5.	000E+00			
A00 9	12.	4770E+014	.9541E+00	1	.2983E+00	-5.	000E+00			
A0010	13.	7280E+017	.4561E+00	1	.6289E+00	-5.	000E+00			
A0011	15.	5623E+011	.1125E+01	2	.0256E+00	-5.	000E+00			
A0012	18.	2433E+011	.6487E+01	2	.5017E+00	-5.	000E+00			
A0013	11.	2152E+022	.4304E+01	3	.0732E+00	-5.	000E+00			
A0014	11.	7838E+023	.5677E+01	3	.7592E+00	-5.	000E+00			
A0015	12.	6097E+025	.2195E+01	4	.5825E+00	-5.	000E+00			
A0016	13.	8076E+027	.6152E+01	5	.5708E+00	-5.	000E+00			
A0017	15.	5429E+021	.1086E+02	6	.7570E+00	-5.	000E+00			
A0018	18.	0546E+021	.6109E+02	8	.1808E+00	-5.	000E+00			
A0019	11.	1687E+032	.3374E+02	9	.8899E+00	-5.	000E+00			
A0020	11.	6937E+033	.3874E+02	1	.1941E+01	-5.	000E+00			
A0021	12.	4521E+034	.9041E+02	1	.4404E+01	-5.	000E+00			
A0022	13.	5470E+037	.0941E+02	1	.7359E+01	-5.	000E+00			
A0023	15.	1275E+031	.0255E+03	2	.0907E+01	-5.	000E+00			
A0024	17.	4080E+031	.4816E+03	2	.5165E+01	-5.	000E+00			
A0025	11.	0698E+042	.1395E+03	3	.0276E+01	-5.	000E+00			
A0026	11.	5442E+043	.0884E+03	3	.6411E+01	-5.	000E+00			
A0027	12.	2284E+044	.4568E+03	4	.3775E+01	-5.	000E+00			
A0028	13.	2148E+046	.4296E+03	5	.2614E+01	-5.	000E+00			
A0029	14.	6368E+049	.2737E+03	6	.3223E+01	-5.	000E+00			

A0030	16.6867E+041.3373E+04	7.5958E+01	-5.000E+00
A0031	19.6412E+041.9282E+04	9.1243E+01	-5.000E+00
A0032	17.5430E+061.5086E+06	2.2363E+02	-5.000E+00
CONNE			
A00 0A00 1	15.0000E-029.160	8E-033.1416E+00	
A00 1A00 2	11.0839E-023.383	4E-024.3982E+00	
A00 2A00 3	15.0188E-024.411	0E-029.6775E+00	
A00 3A00 4	15.6743E-025.466	5E-021.6014E+01	
A00 4A00 5	16.6390E-026.672	9E-022.3620E+01	
A00 5A00 6	17.8574E-028.092	3E-023.2750E+01	
A00 6A00 7	19.3486E-029.779	8E-024.3708E+01	
A00 7A00 8	11.1155E-011.179	5E-015.6862E+01	
A00 8A00 9	11.3333E-011.420	8E-017.2650E+01	
A00 9A0010	11.5954E-011.709	9E-019.1601E+01	
A0010A0011	11.9104E-012.056	6E-011.1435E+02	
A0011A0012	12.2890E-012.472	4E-011.4165E+02	
A0012A0013	12.7436E-012.971	4E-011.7443E+02	
A0013A0014	13.2894E-013.570	1E-012.1376E+02	
A0014A0015	13.9448E-014.288	7E-012.6098E+02	
A0015A0016	14.7315E-015.151	1E-013.1766E+02	
A0016A0017	15.6760E-016.186	2E-013.8569E+02	
A0017A0018	16.8097E-017.428	6E-014.6734E+02	
A0018A0019	18.1706E-018.919	8E-015.6535E+02	
A0019A0020	19.8041E-011.071	0E+006.8300E+02	
A0020A0021	11.1765E+001.285	8E+008.2421E+02	
A0021A0022	11.4118E+001.543	37E+009.9371E+02	
A0022A0023	11.6943E+001.853	32E+001.1972E+03	
A0023A0024	12.0334E+002.224	7E+001.4414E+03	
A0024A0025	12.4405E+002.670	7E+001.7345E+03	
A0025A0026	12.9290E+003.205	9E+002.0863E+03	
A0026A0027	13.5154E+003.848	4E+002.5086E+03	
A0027A0028	14.2193E+004.619	6E+003.0156E+03	
A0028A0029	15.0642E+005.545	2E+003.6240E+03	
A0029A0030	16.0784E+006.656	3E+004.3543E+03	
A0030A0031	17.2956E+007.989	9E+005.2310E+03	
A0031A0032	18.7567E+001.236	3E+026.2832E+03	

```
GENER----1----*----2----*----3----*----4----*----5----*----6----*----8
A00 0WW001
                             MASS -1.00E-02
                             MASS -1.00E-02
A0020WW002
A0025WW003
                             MASS -1.00E-02
INCON----1----*----2----*----4----*----5----*---6----*----8
SUBDOMAINS----*----2----*-----4----*----5----*----6----*-----8
&Subdomain General Info number of subdomains = 1 /
  &Individual Subdomain Specifics subdomain name = 'WellZ',
                              number of regions = 1
     &Region Specifics definition mode = 'NameList',
                     number of elements = 7,
                     format to read data = '*',
'A00 1' 'A00 2' 'A00 3' 'A00 4' 'A00 5' 'A00 6' 'A00 7'
&Interface General Info number of interfaces = 1 /
  &Individual Interface Specifics interface name
                                                  = 'IntRR',
                              number of surfaces = 1,
                              sign of flow direction = 'DIR'
     &Surface Specifics definition mode
                                        = 'NameList',
                      number of connections = 1,
                                                       ! Range (min and max) along the first coordinate axis
                      format to read data = '*',
                      1
'A00 4A00 5'
&SSGroup General Info number of SSGroups = 1 /
  &Individual SSGroup Specifics SSGroup name
                                             = 'Wells',
                             definition mode
                                             = 'NameList',
                             number of SS
                                             = 3,
                             format to read data = '*' !... '(3(A5,1x))'
                             1
'WW001' 'WW002' 'WW003'
ENDCY----1----*----2----*----3----*----4----*----5----*----6----*----8
```

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